



# Measurement of the Proton Polarizabilities at MAMI



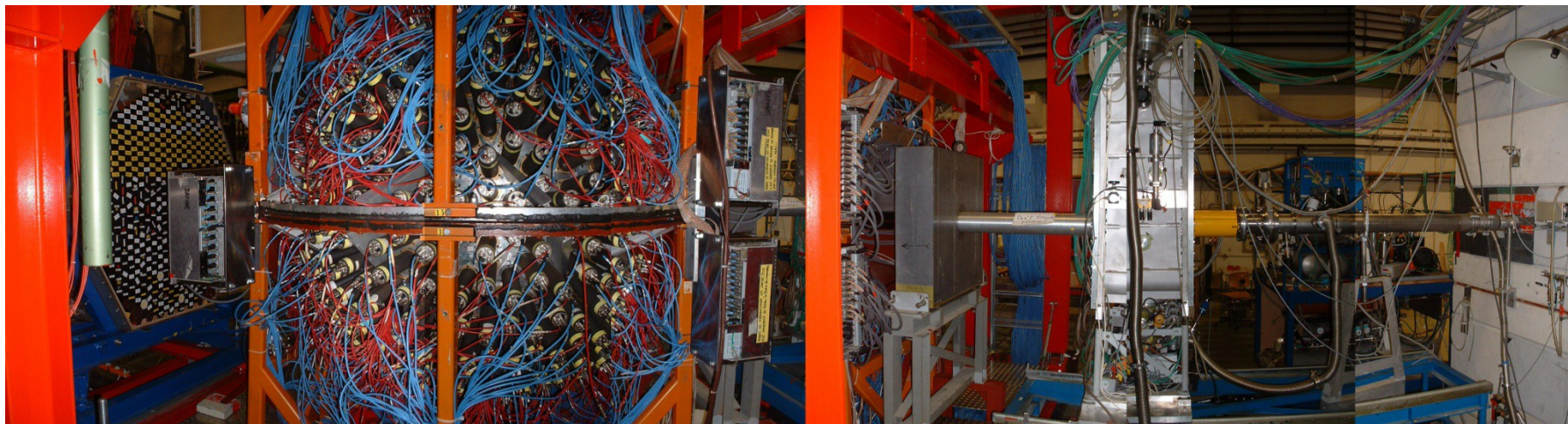
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WASHINGTON, DC

**Vahe Sokhoyan**  
**for the A2 Collaboration**



DPG Meeting, Frankfurt  
21.03.2014



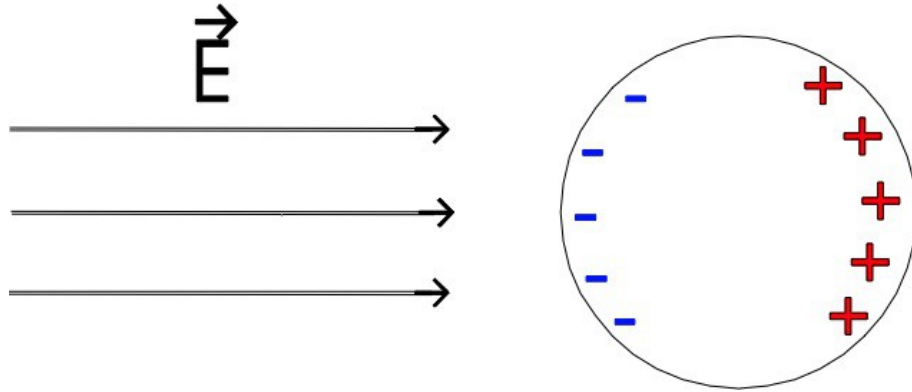
# Contents

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- Scalar and spin polarizabilities
- Compton scattering on the proton
- Experimental setup
- Results
- Ongoing work and future plans
- Summary and outlook

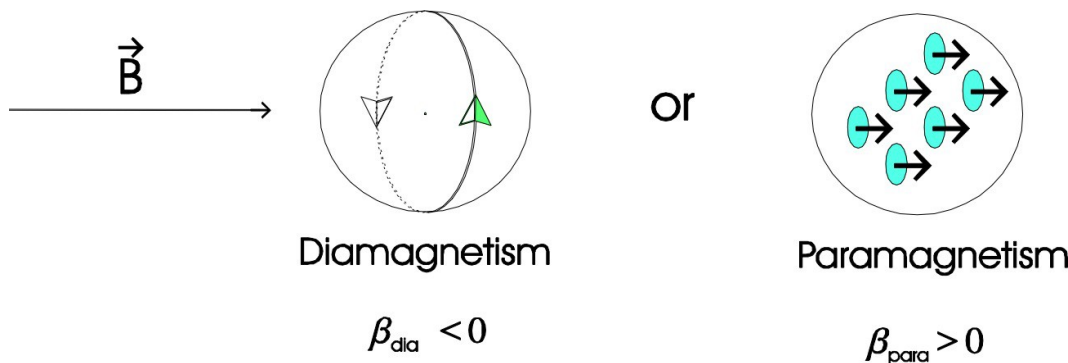
# Scalar polarizabilities

## Proton Electric Polarizability



- $\alpha_{E1}$ : electric polarizability
- Proton between charged parallel plates: “stretchability”

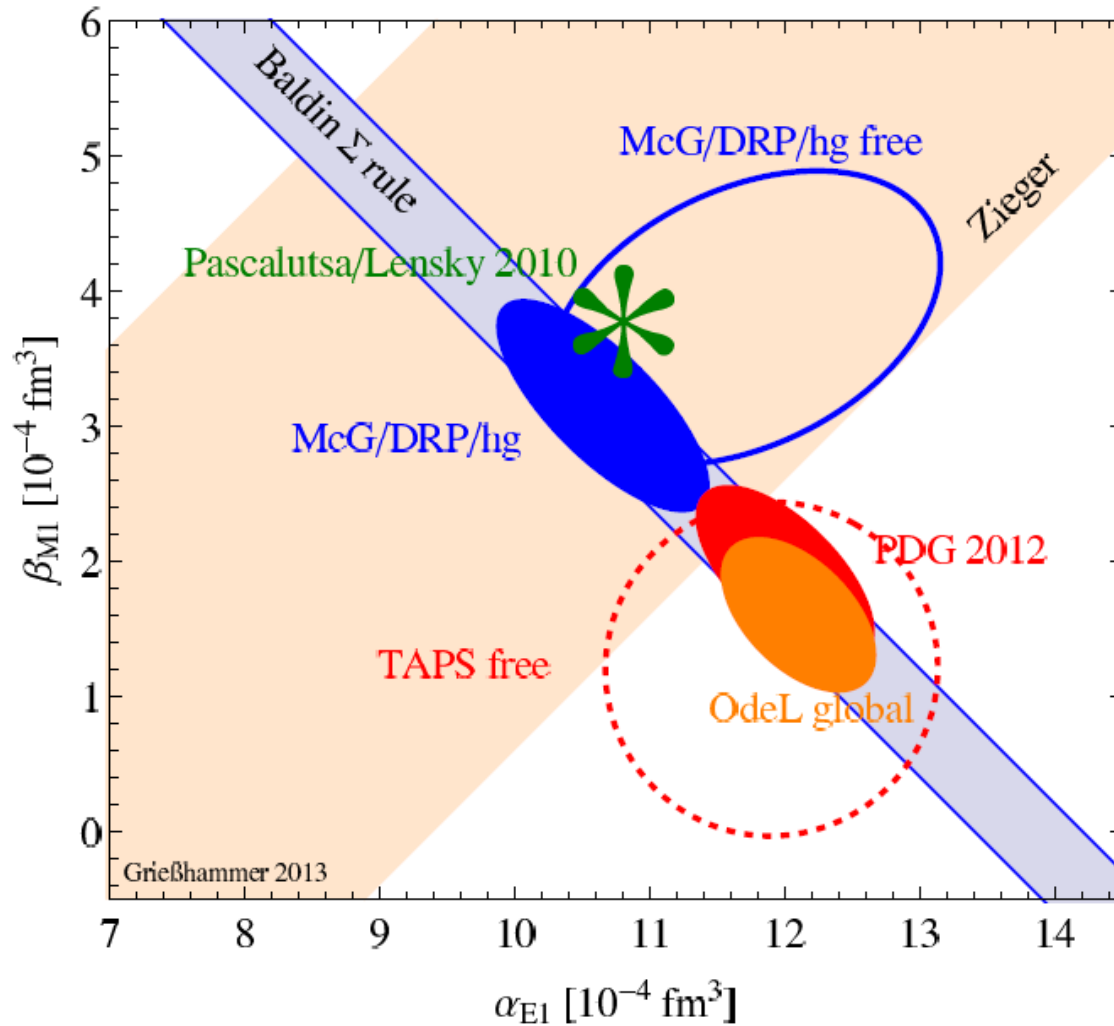
## Proton Magnetic Polarizability



- $\beta_{M1}$ : magnetic polarizability
- Proton between poles of a magnet: “alignability”

- Fundamental properties of the proton
- Important to astrophysics, atomic physics, spin polarizability measurements, etc.

# Existing data and model predictions

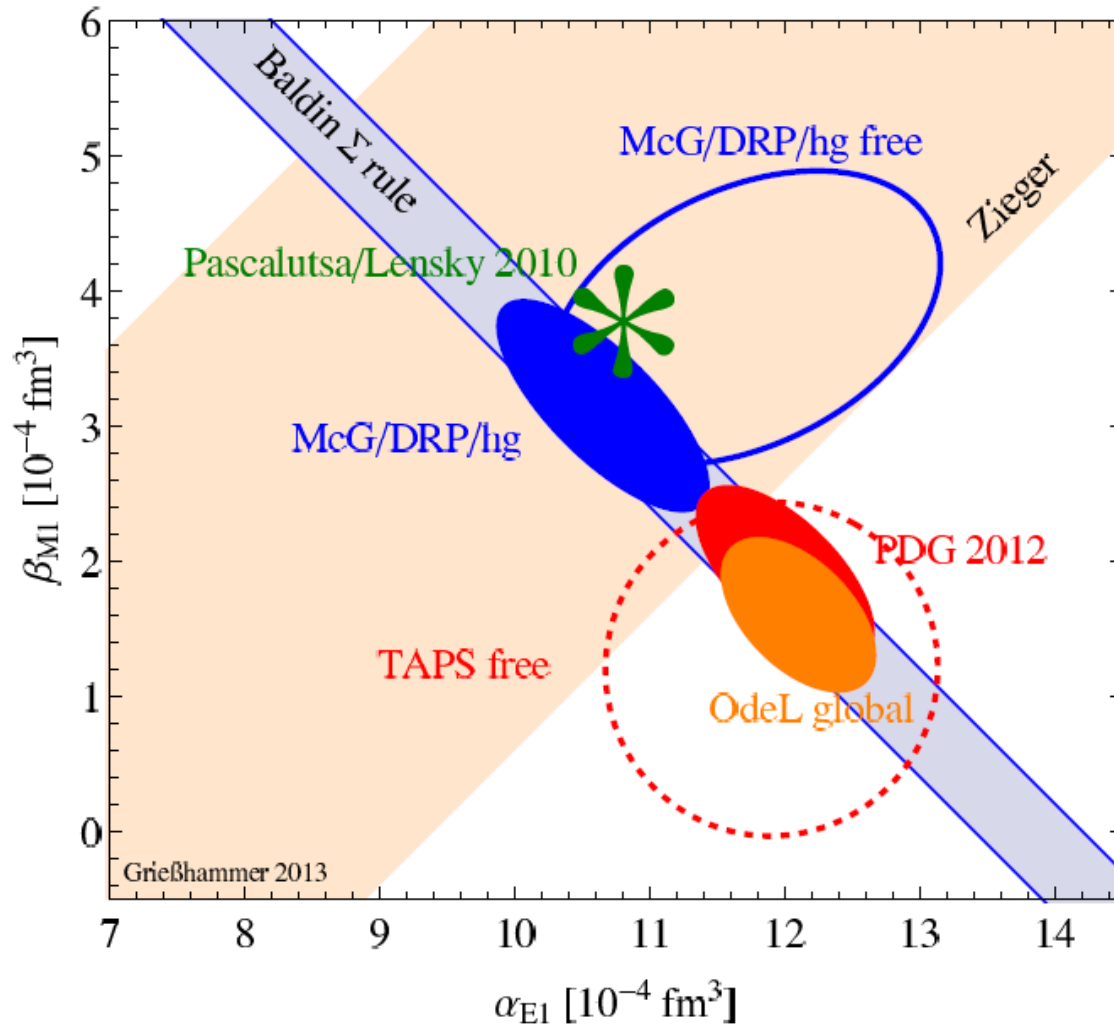


**PDG (2012) values:**

$$\alpha_{E1} = (12.0 \pm 0.6) \times 10^{-4} \text{ fm}^3$$

$$\beta_{M1} = (1.9 \pm 0.5) \times 10^{-4} \text{ fm}^3$$

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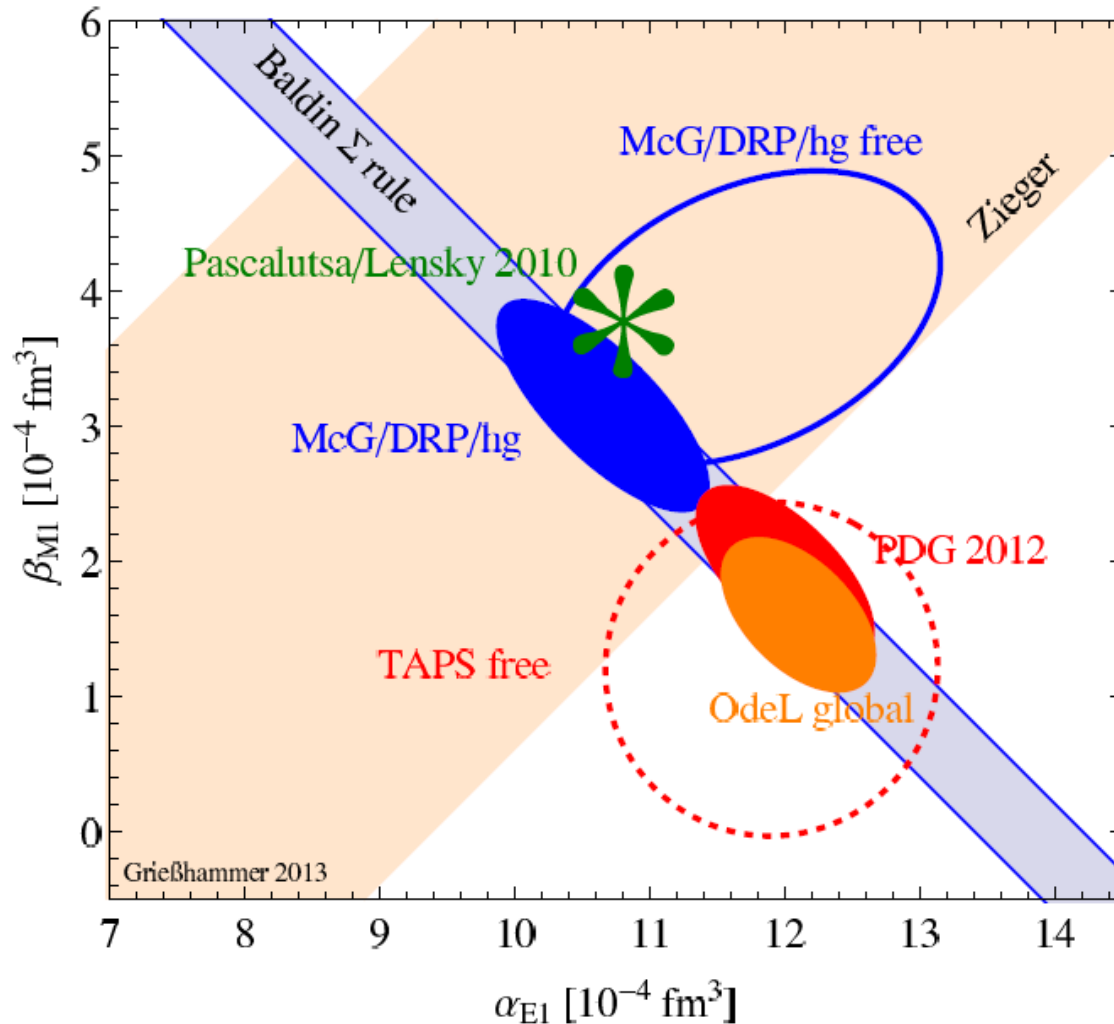
$$\beta_{M1} = (1.9 \pm 0.5) \times 10^{-4} \text{ fm}^3$$

## New (2013) PDG values:

$$\alpha_{E1} = (11.2 \pm 0.4) \times 10^{-4} \text{ fm}^3$$

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**Significant change between reviews without introducing new experimental data? New quality data needed!**

**In the low energy range  $\Sigma_3$  is purely dependent on  $\beta$**

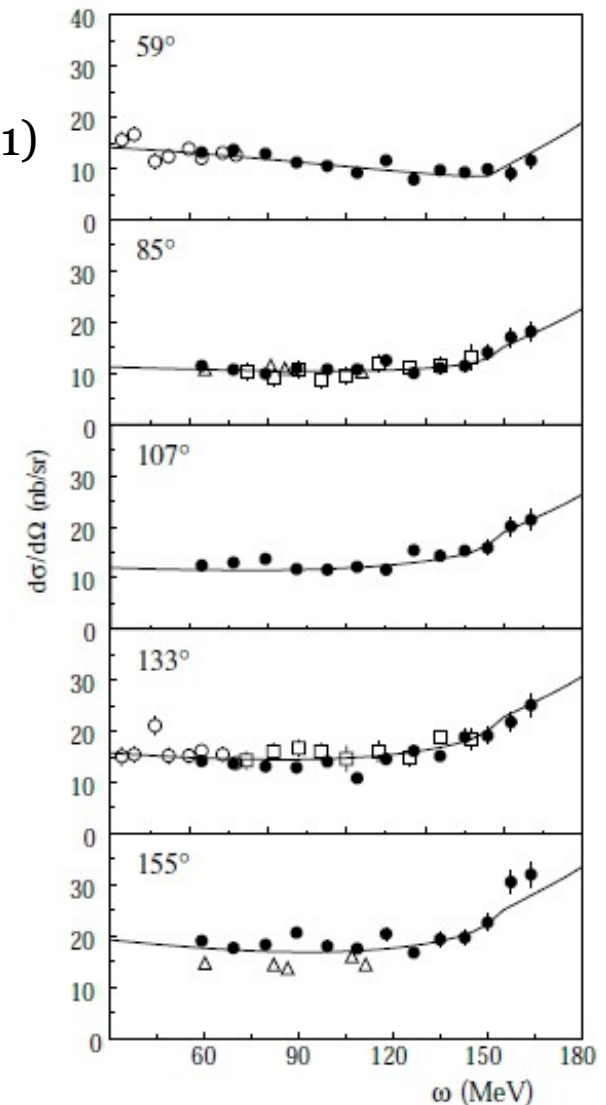
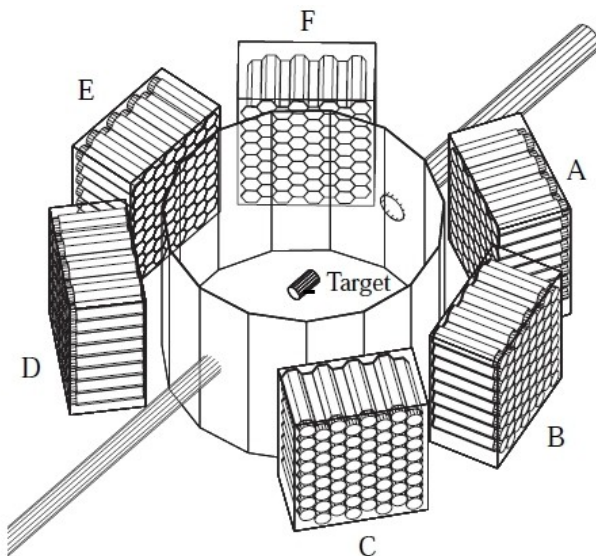
Krupina and Pascalutsa, PRL 110, 262001 (2013)

**Talk of N. Krupina (this session)**



# Existing data

- Highest statistics data set:  
V. Olmos de Leon et al. Eur. Phys. J. A 10, 207–215 (2001)
- 200 hours of Compton scattering
- 20 cm  $\text{IH}_2$  target with TAPS
- 180 MeV electron beam
- $E_\gamma = 55\text{--}165$  MeV,  $59^\circ < \Theta < 155^\circ$
- 1/3 acceptance of CB System!



Triangles: P.S. Baranov et al., Phys. Lett. B 52, 22 (1974);  
P.S. Baranov et al., Sov. J. Nucl. Phys. 21, 355 (1975)  
Open circles: F.J. Federspiel et al., Phys. Rev. Lett. 67, 1511 (1991)  
Squares B.E. MacGibbon et al., Phys. Rev. C 52, 2097 (1995)  
Curve: R.A. Arndt et al., Phys. Rev. C 53, 430 (1996)

# Measurement of $\alpha$ and $\beta$

Originally suggested measurement: cross section difference between linearly polarized photons parallel and perpendicular to reaction plane

$$\frac{d\sigma^{\perp} - d\sigma^{\parallel}}{d\Omega}$$

proportional to  $\alpha$

$$z = \cos \theta$$

$$\frac{z^2 d\sigma^{\perp} - d\sigma^{\parallel}}{d\Omega}$$

proportional to  $\beta$

➡ **Independent** extraction of  $\alpha$  &  $\beta$  possible!



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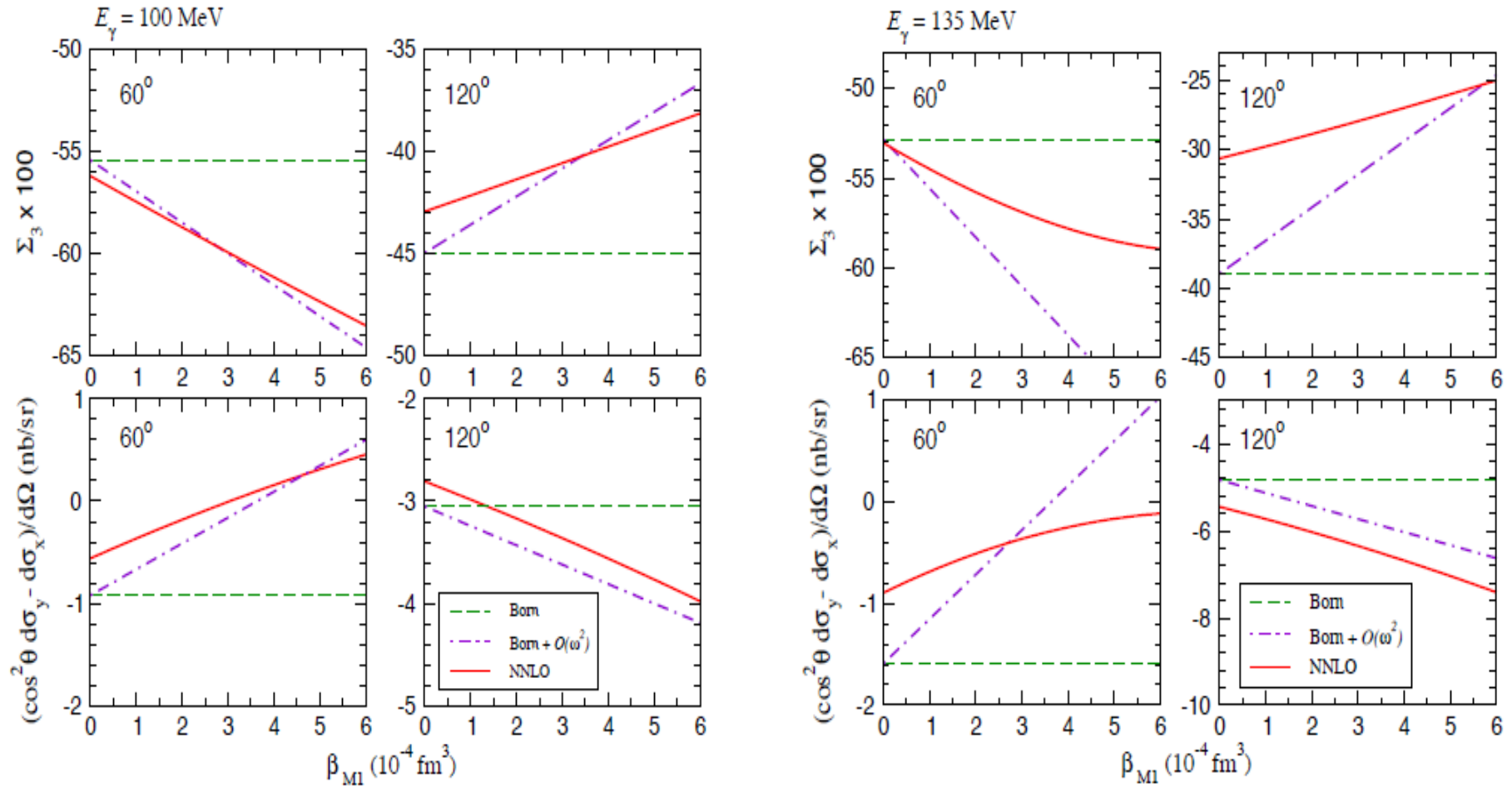
$$\frac{z^2 d\sigma^{\perp} - d\sigma^{\parallel}}{d\Omega}$$

proportional to  $\beta$

- ➔ **Independent** extraction of  $\alpha$  &  $\beta$  possible!
- ➔ New work by Krupina and Pascalutsa [PRL 110, 262001 (2013)]
- ➔ At low energies, the beam asymmetry,  $\Sigma_3$ , is the best way to extract  $\beta$

$$\Sigma_3 \equiv \frac{d\sigma^{\perp} - d\sigma^{\parallel}}{d\sigma^{\perp} + d\sigma^{\parallel}}$$

# Measurement of $\alpha$ and $\beta$



Krupina and Pascalutsa, PRL 110, 262001 (2013)

# Systematical cross-checks

Goal: Determination of  $\alpha$  and  $\beta$

- We measure  $\sigma_{\perp}$ ,  $\sigma_{\parallel}$ ,  $\sigma_{\text{unpol}}$

$$\frac{d\sigma}{d\Omega}(\theta, \phi) = \frac{d\sigma}{d\Omega}(\theta) [1 + p_{\gamma} \Sigma_3 \cos(2\phi)]$$

- Measurement of the beam asymmetry  $\Sigma_3$

$$\Sigma_3 = \frac{d\sigma^{\perp} - d\sigma^{\parallel}}{d\sigma^{\perp} + d\sigma^{\parallel}}$$

- Measurement of absolute cross-sections
- Challenging with linearly polarized beam

# Spin polarizabilities

- These parameters describe the response of the proton spin to an applied electric or magnetic field
- Nucleon has 4 spin or vector polarizabilities:

$$\gamma_{E1E1} \quad \gamma_{M1M1} \quad \gamma_{M1E2} \quad \gamma_{E1M2}$$

- Intimately connected to the nucleon's spin structure:

**Fundamental properties of the proton!**

- Higher order in incident-photon energy, small effect at lower energies
- Need theoretical help in extracting values

# Spin polarizabilities

$\gamma$	Theory					Experiment
	$p^4\text{HB}$	$\epsilon^3\text{SSE}$	NNLO	DRs	Kmatrix	
$E1E1$	-1.4	-5.4	-4.5	-4.3	-5.0	no data
$M1M1$	3.3	1.4	3.7	2.9	3.4	no data
$E1M2$	0.2	1.0	-0.9	0.0	-1.8	no data
$M1E2$	1.8	1.0	2.2	2.1	1.1	no data
0	-3.9	2.0	-0.7	-0.7	2.3	$-1.01 \pm 0.08 \pm 0.13$
$\pi$	6.3	6.8	11.3	9.3	11.3	$8.0 \pm 1.8$

- Proton spin polarizability predictions and measurements in units of  $10^{-4} \text{ fm}^4$
- Note the large absolute error on  $\gamma_\pi$

→ Forward spin polarizability has been determined by a “GDH-type” of sum rule

$$\gamma_0 = -\gamma_{E1E1} - \gamma_{M1M1} - \gamma_{E1M2} - \gamma_{M1E2}$$

→ Backward spin polarizability has been determined from a dispersive analysis of backward-angle Compton scattering

$$\gamma_\pi = -\gamma_{E1E1} + \gamma_{M1M1} - \gamma_{E1M2} + \gamma_{M1E2}$$

# Spin polarizabilities

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## What to do?

- Use Compton scattering to probe them!
- Measurements with polarized photons and targets
- Low sensitivity at low energies, so we need higher energies, into  $\Delta$  region
- Three asymmetries,  $\Sigma_3$ ,  $\Sigma_{2x}$ , and  $\Sigma_{2z}$  were chosen to obtain the spin polarizabilities of the proton



# Asymmetries

1. Beam: circular, Target: longitudinal

$$\Sigma_{2z} = \frac{\sigma_{+z}^R - \sigma_{+z}^L}{\sigma_{+z}^R + \sigma_{+z}^L} = \frac{\sigma_{+z}^R - \sigma_{-z}^R}{\sigma_{+z}^R + \sigma_{-z}^R}$$

2. Beam: circular, Target: transverse

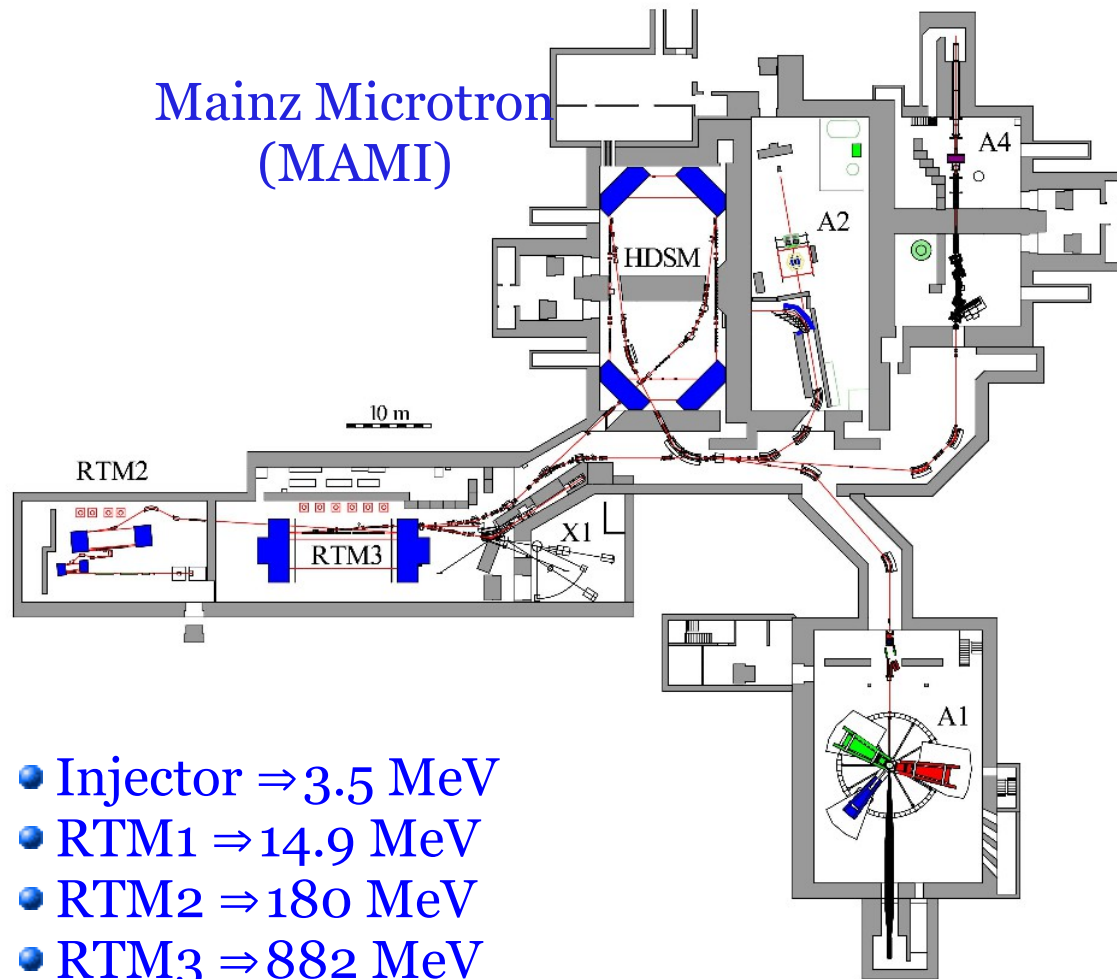
$$\Sigma_{2x} = \frac{\sigma_{+x}^R - \sigma_{+x}^L}{\sigma_{+x}^R + \sigma_{+x}^L} = \frac{\sigma_{+x}^R - \sigma_{-x}^R}{\sigma_{+x}^R + \sigma_{-x}^R}$$

3. Beam: linear, parallel and perpendicular to scattering plane  
Target: unpolarized

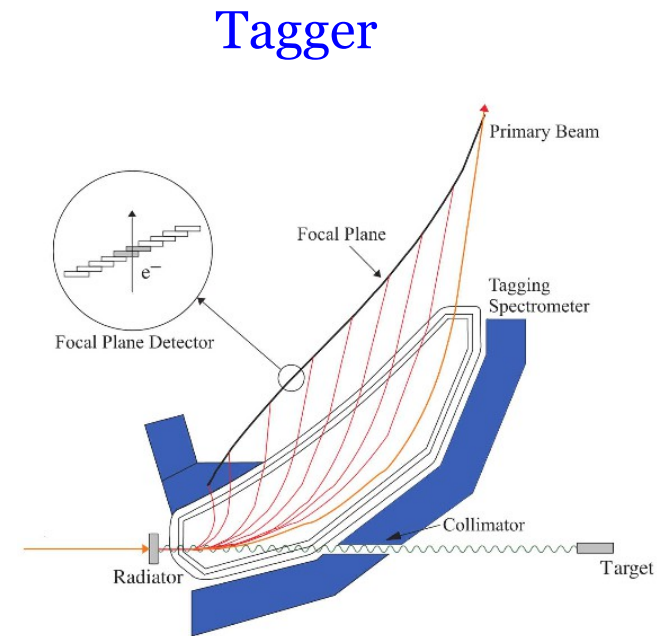
$$\Sigma_3 = \frac{\sigma^{\parallel} - \sigma^{\perp}}{\sigma^{\parallel} + \sigma^{\perp}}$$

By measuring three asymmetries at different energies and angles, we can conduct an in-depth global analysis to extract **all four spin polarizabilities** with small statistical, systematic, and model-dependent errors  
(R.Miskimen, P.Martel, A. Mushkarenkov)

# Experimental setup



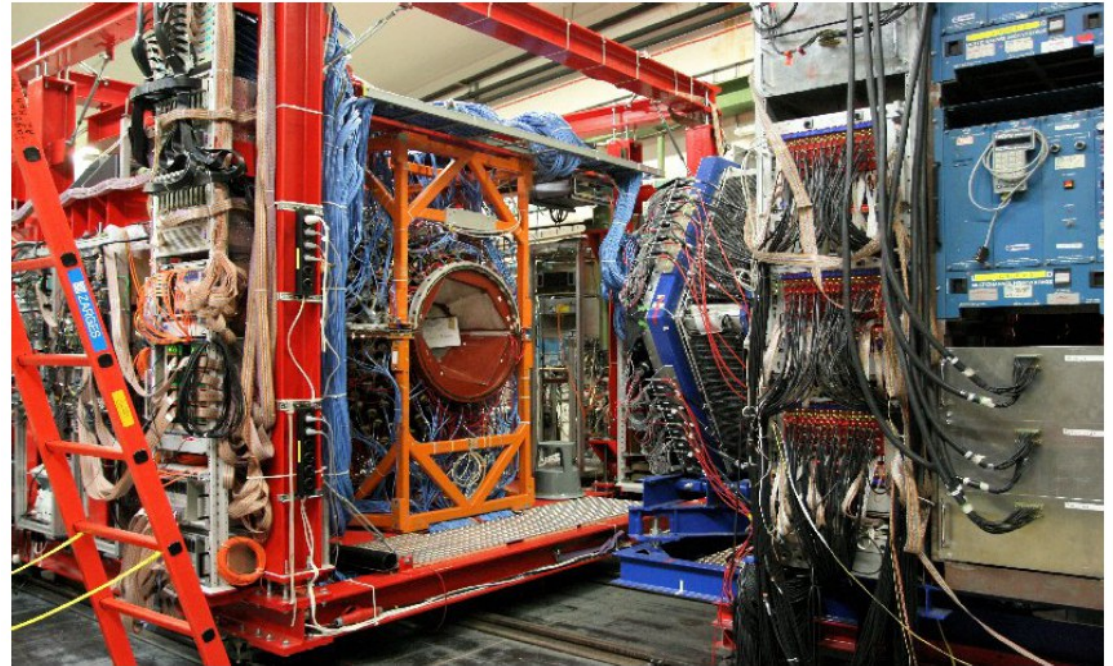
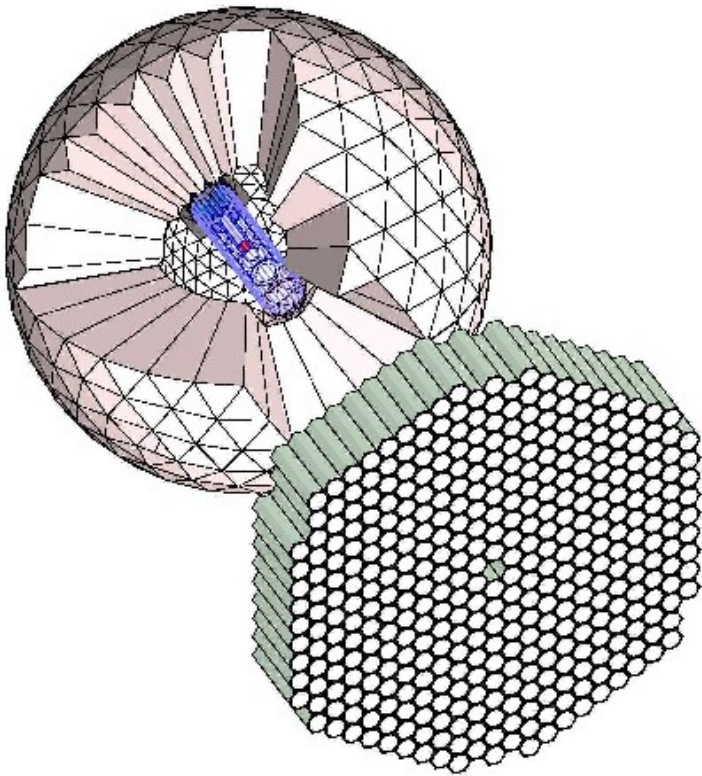
- Injector  $\Rightarrow 3.5$  MeV
- RTM1  $\Rightarrow 14.9$  MeV
- RTM2  $\Rightarrow 180$  MeV
- RTM3  $\Rightarrow 882$  MeV
- HDSM  $\Rightarrow 1.6$  GeV



$$E_{\gamma} = E_o - E_{e^-}$$

- ➡ High-Flux, Tagged, Bremsstrahlung Photon Beam: Unpolarized, Linear, and Circular
- ➡ Polarized and Unpolarized Targets

# Experimental setup



## **Crystal Ball:**

- 672 NaI Crystals
- 24 Particle Identification Detector Paddles
- 2 Multiwire Proportional Chambers

## **TAPS:**

- 366 BaF<sub>2</sub> and 72 PbWO<sub>4</sub> Crystals
- 384 Veto Detectors

# Selection

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## Selection of $\gamma p \rightarrow \gamma p$ at low energies:

- $E_{\gamma(\text{beam})} = 80 - 150 \text{ MeV}$
- Selecting events with 1  $\gamma$
- Proton does not reach detectors at low energies
- $E_\gamma$  cuts determined from MC
- Missing mass cut
- Subtraction of random timing background
- Subtraction of empty target contribution
- Comparison with Monte Carlo

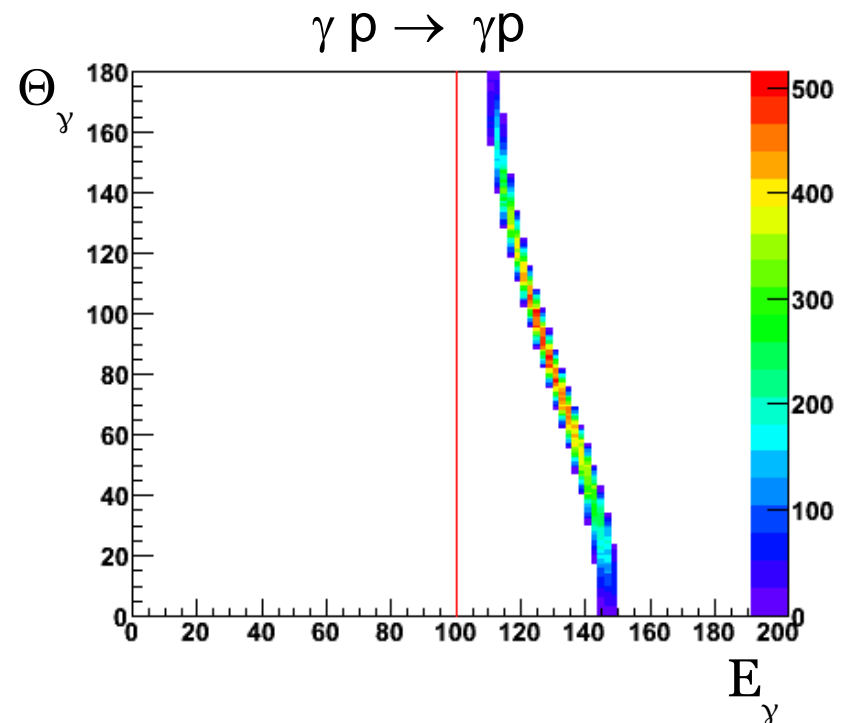
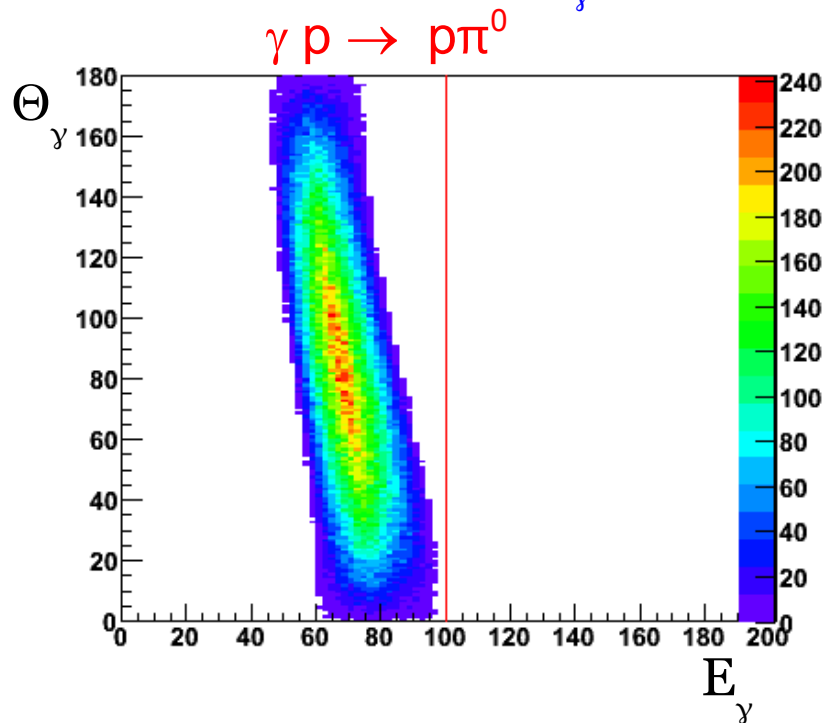
# Elimination of $\pi^0$ background

- Main background source for Compton scattering:  $\gamma p \rightarrow p\pi^0$
- Background production mechanism: 1  $\gamma$  lost
- Kinematics similar to Compton scattering
- Significantly ( $\sim 100$  times) higher cross-section

**Low energy range:**

→ Can be removed at  $\sim 150$  MeV (e.g. 145 – 150 MeV)

→ Cut on  $E_\gamma$

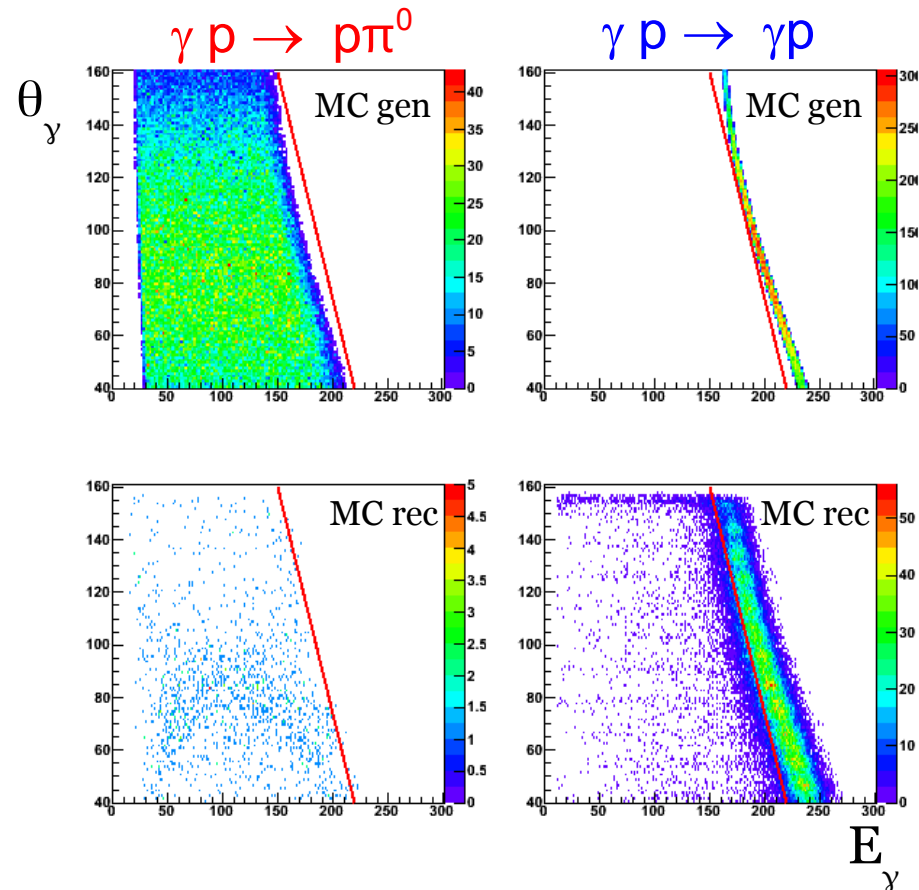


# Elimination of $\pi^0$ background

- Main background source for Compton scattering:  $\gamma p \rightarrow p\pi^0$
- Background production mechanism: 1  $\gamma$  lost
- Kinematics similar to Compton scattering
- Significantly higher cross-section
- Higher energies: 1  $\gamma$  can take the largest part of the  $\pi^0$  energy

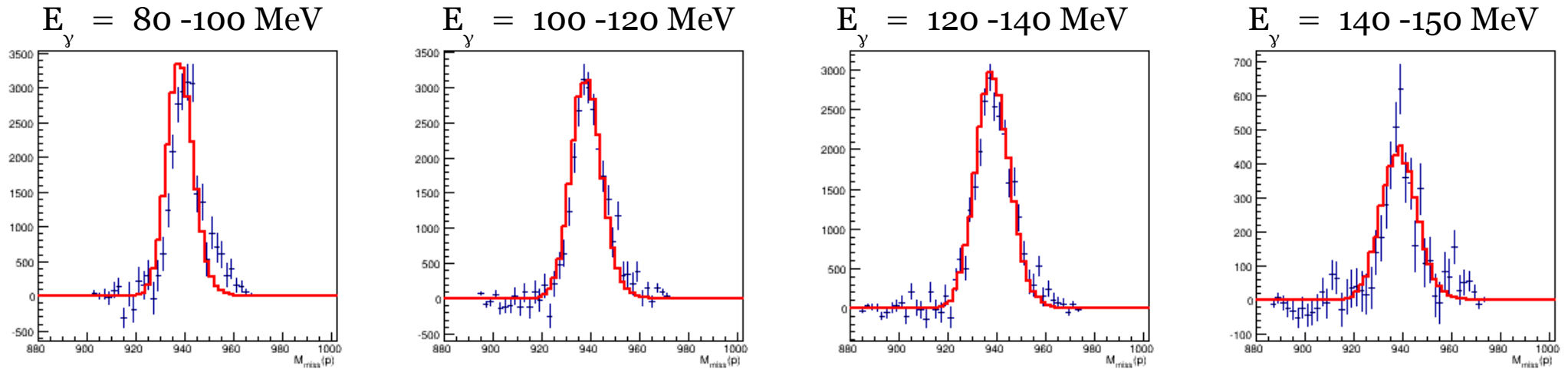
Up to  $\sim 250$  MeV:  
2D (E,  $\theta$ ) cut!

$E_\gamma = 245\text{-}255$  MeV





# Comparison with Monte Carlo



Red: Monte Carlo, Blue: Data

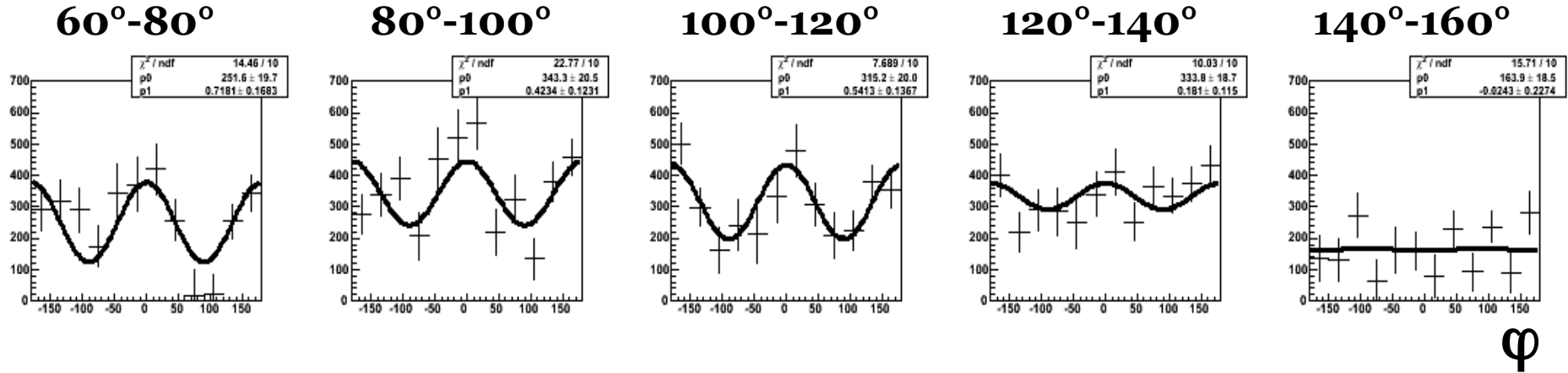
$$\Theta_{\gamma} = 60^{\circ} - 160^{\circ}$$

- Good agreement between data and Monte Carlo
- Low background contamination in all energy bins

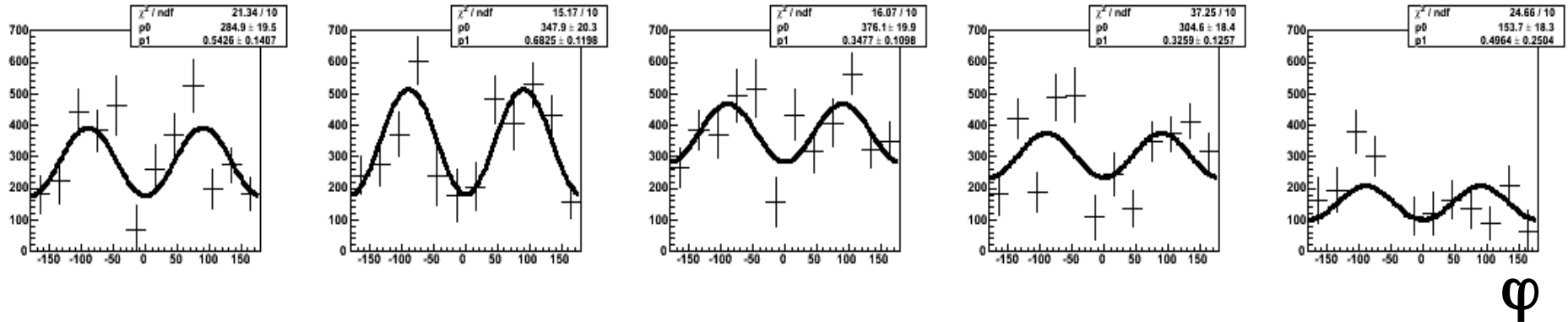
**Preliminary**

# Preliminary asymmetries ( $E_\gamma = 120 - 140$ MeV)

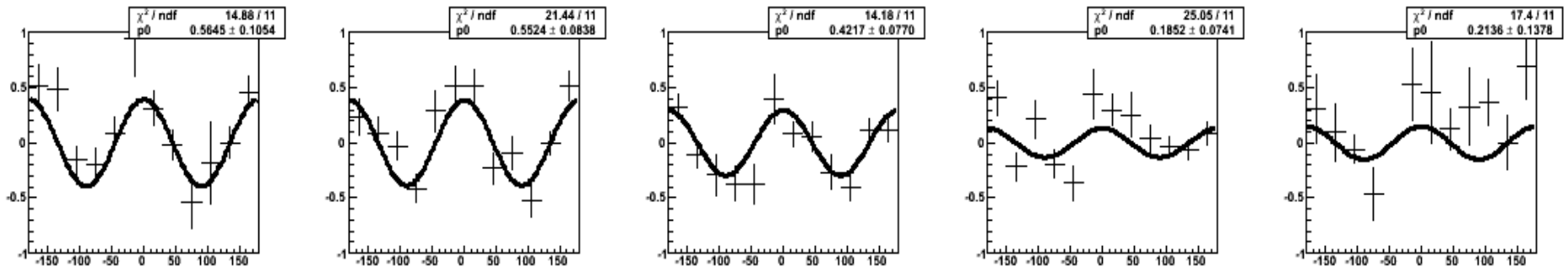
PERP



PARA



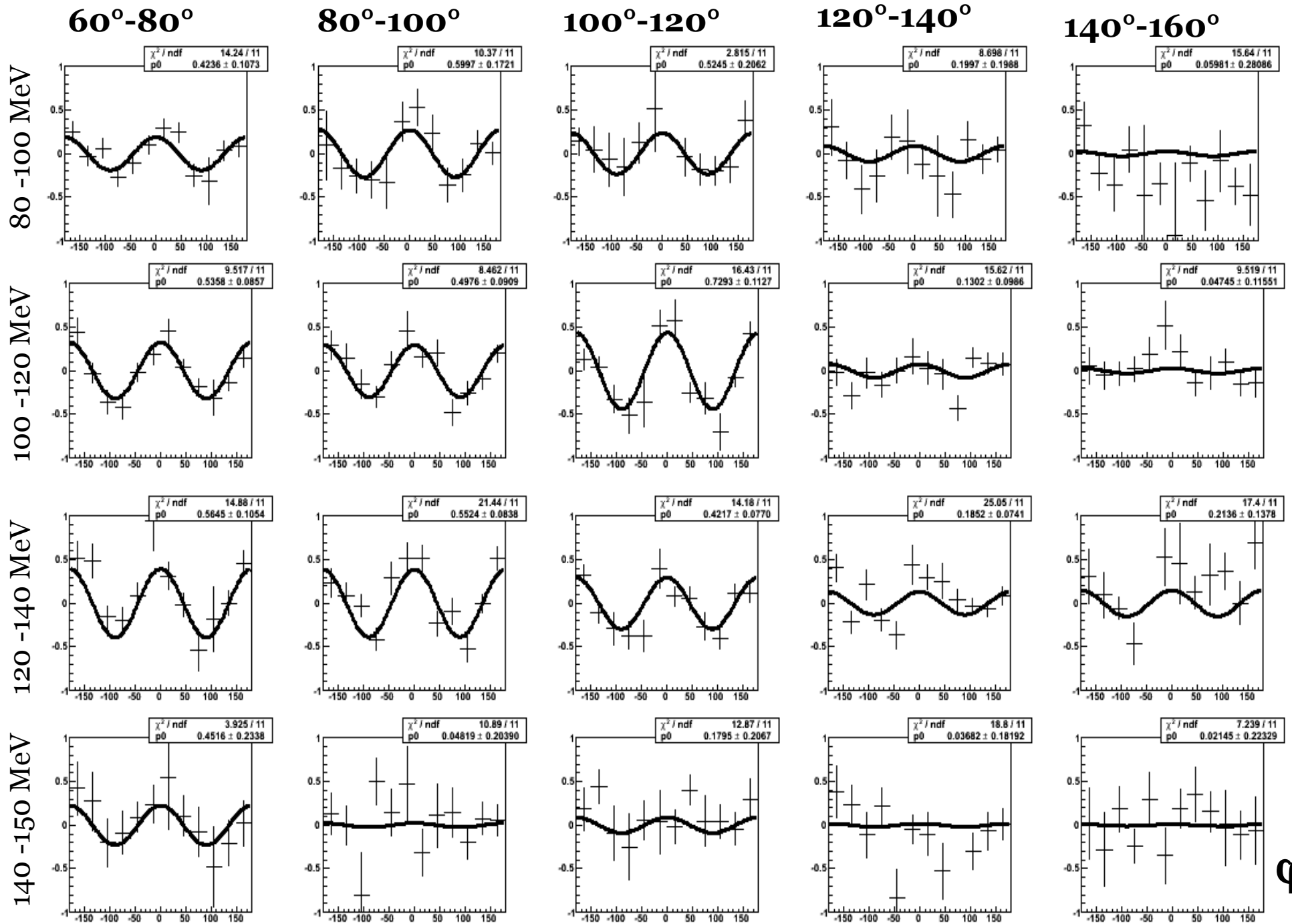
(PERP - PARA) /  
(PERP + PARA)



Preliminary

Binning in  $\Theta_\gamma$

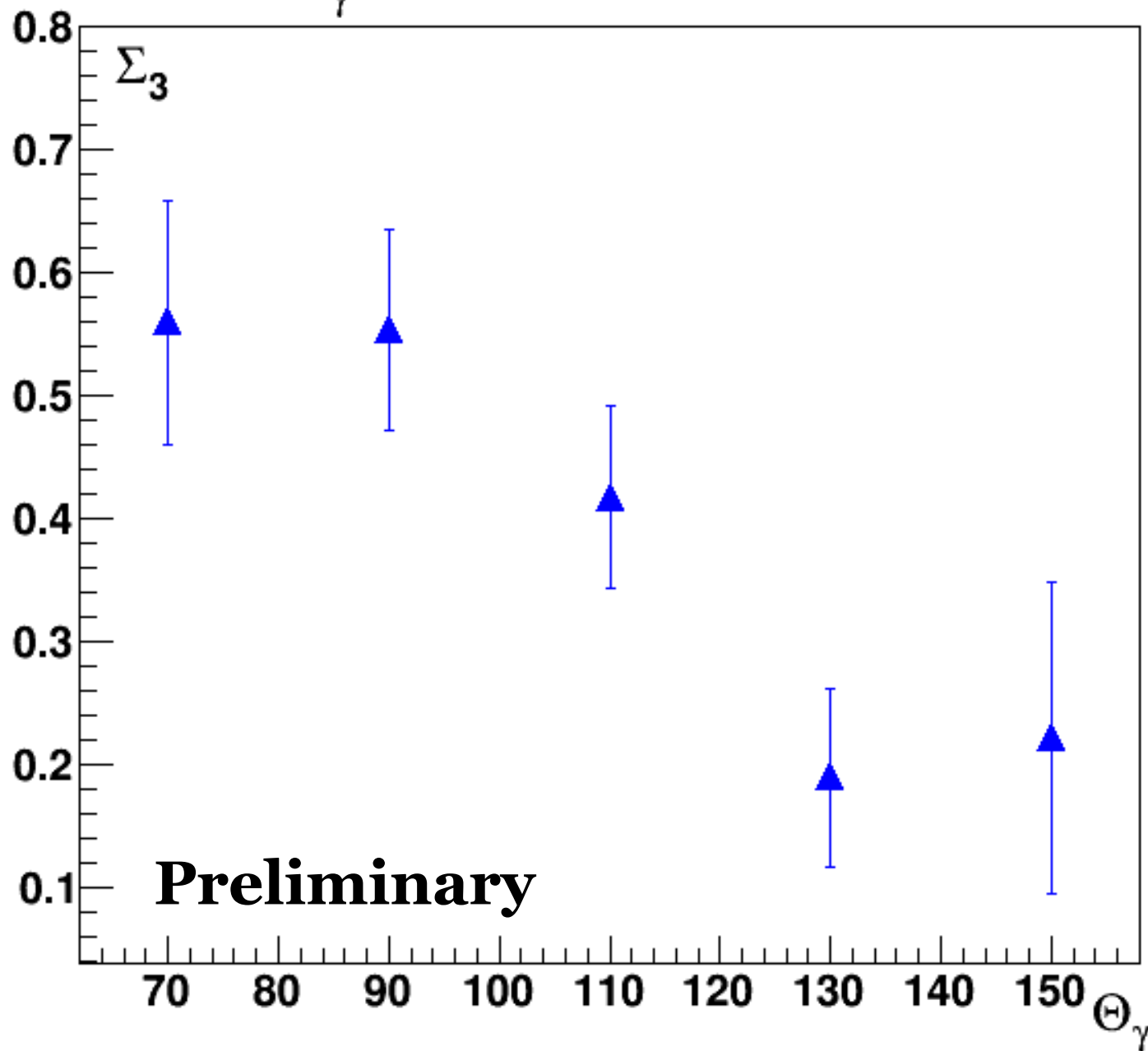
# Preliminary asymmetries



$\varphi$

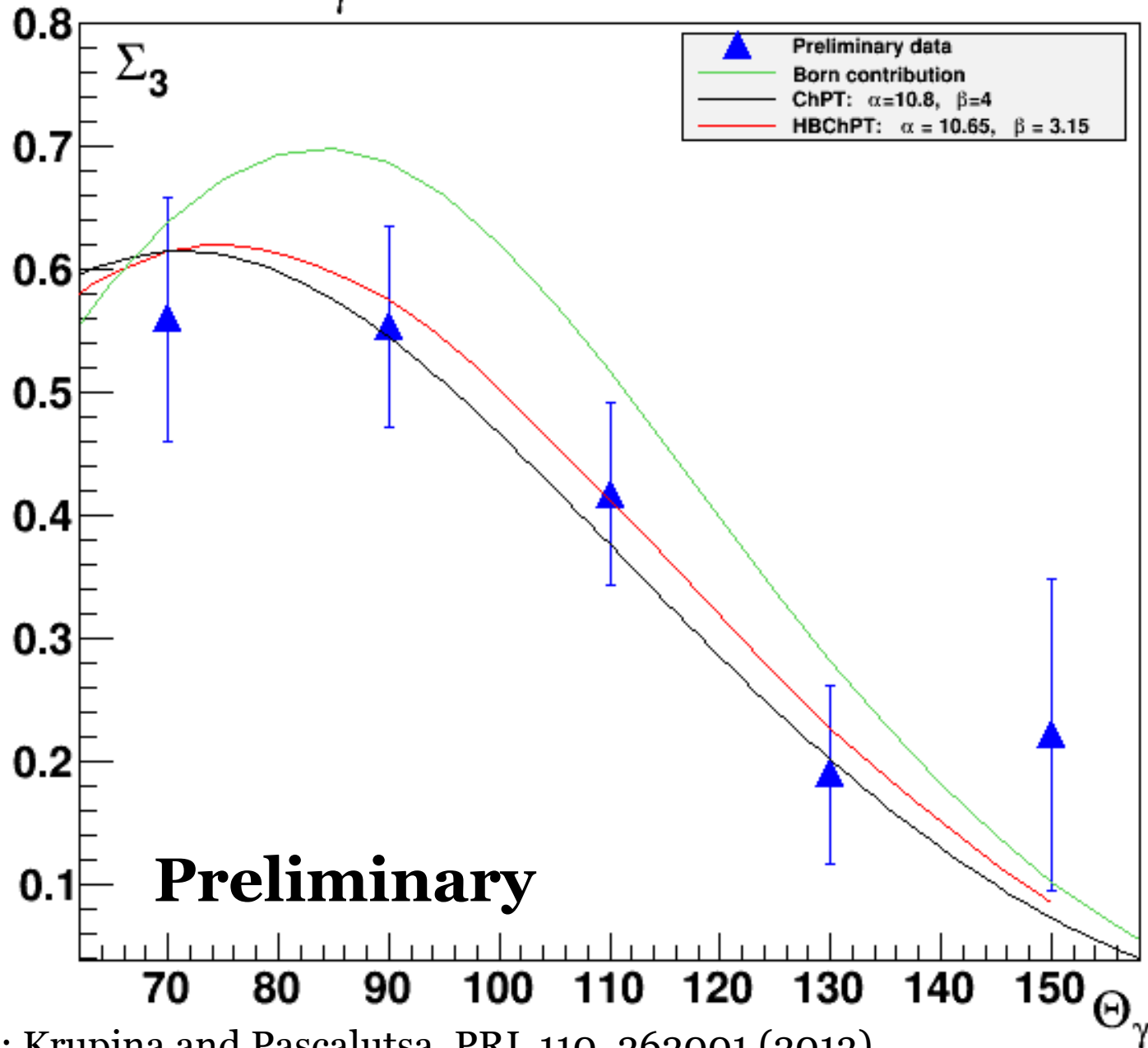
# $\Sigma_3$ : Preliminary results

$E_\gamma = 120 - 140 \text{ MeV}$



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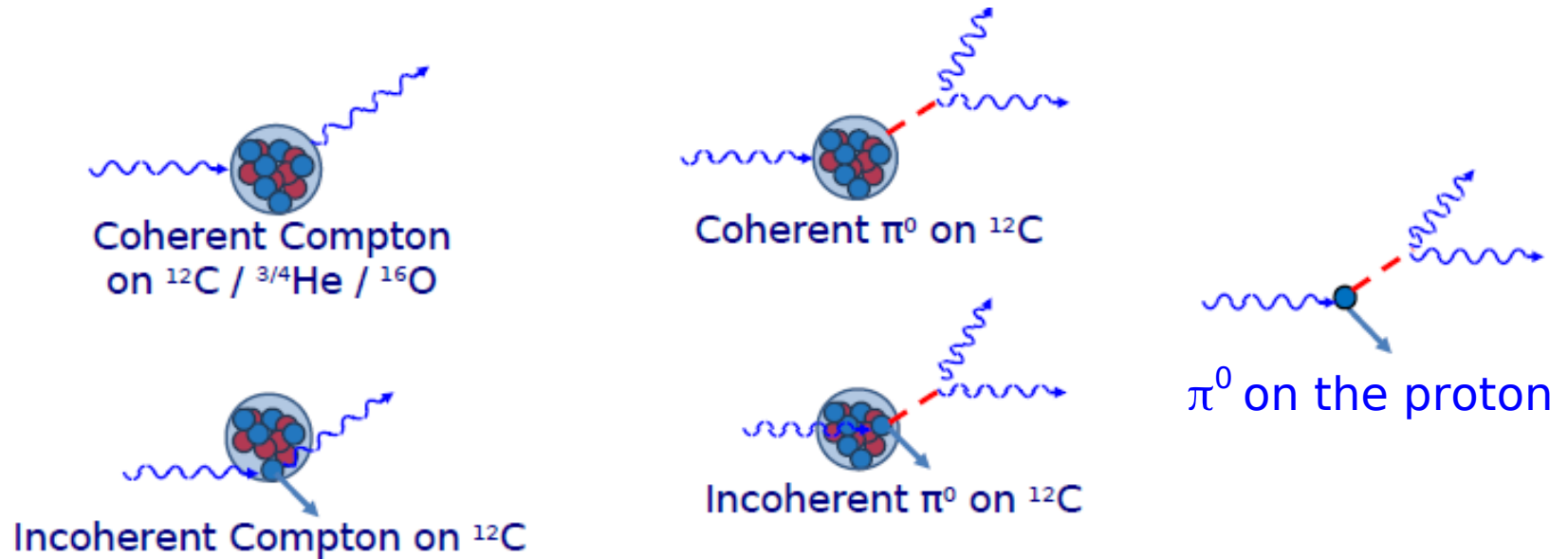
$E_\gamma = 120 - 140 \text{ MeV}$



Curves: Krupina and Pascalutsa, PRL 110, 262001 (2013),  
J. McGovern, D. Phillips, H. Griebhammer, EPJA 49, 12 (2013)

# $\Sigma_{2x}$ : Experimental challenges

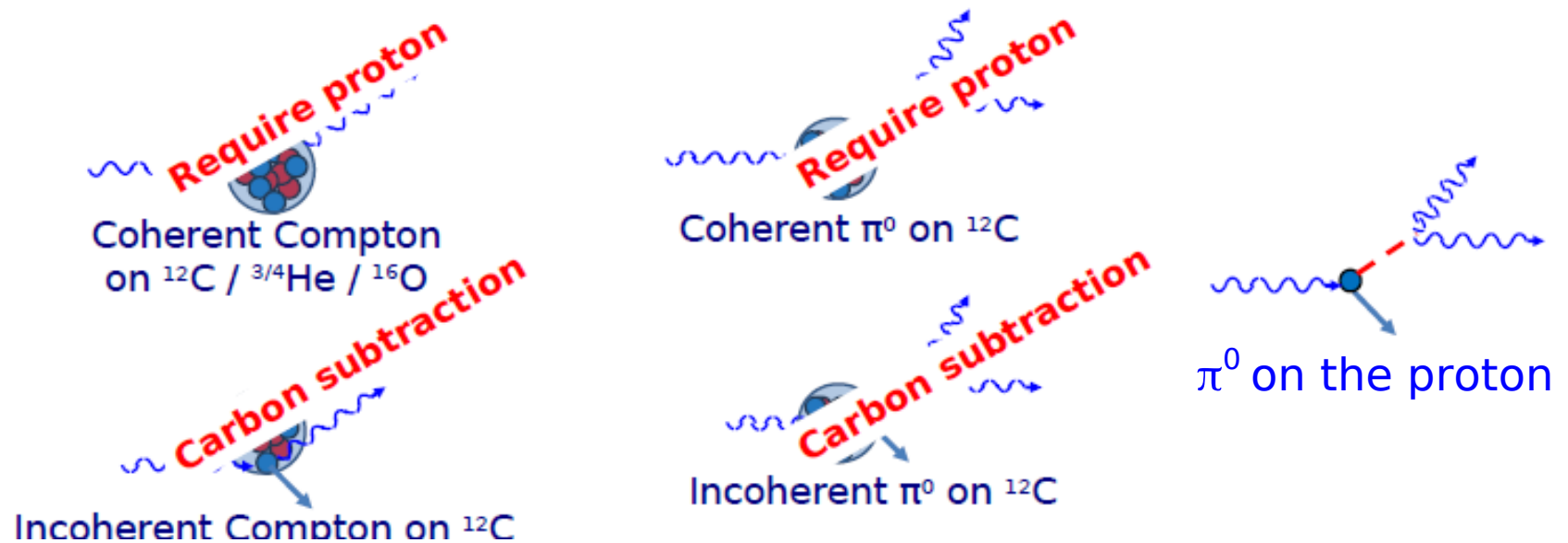
- Small Compton scattering cross sections
- Large backgrounds
- Butanol target ( $C_4H_9OH$ ): Coherent and incoherent reactions off C, O and He
- Proton tracks are required to suppress backgrounds, but energy losses e.g. in the target are considerable.





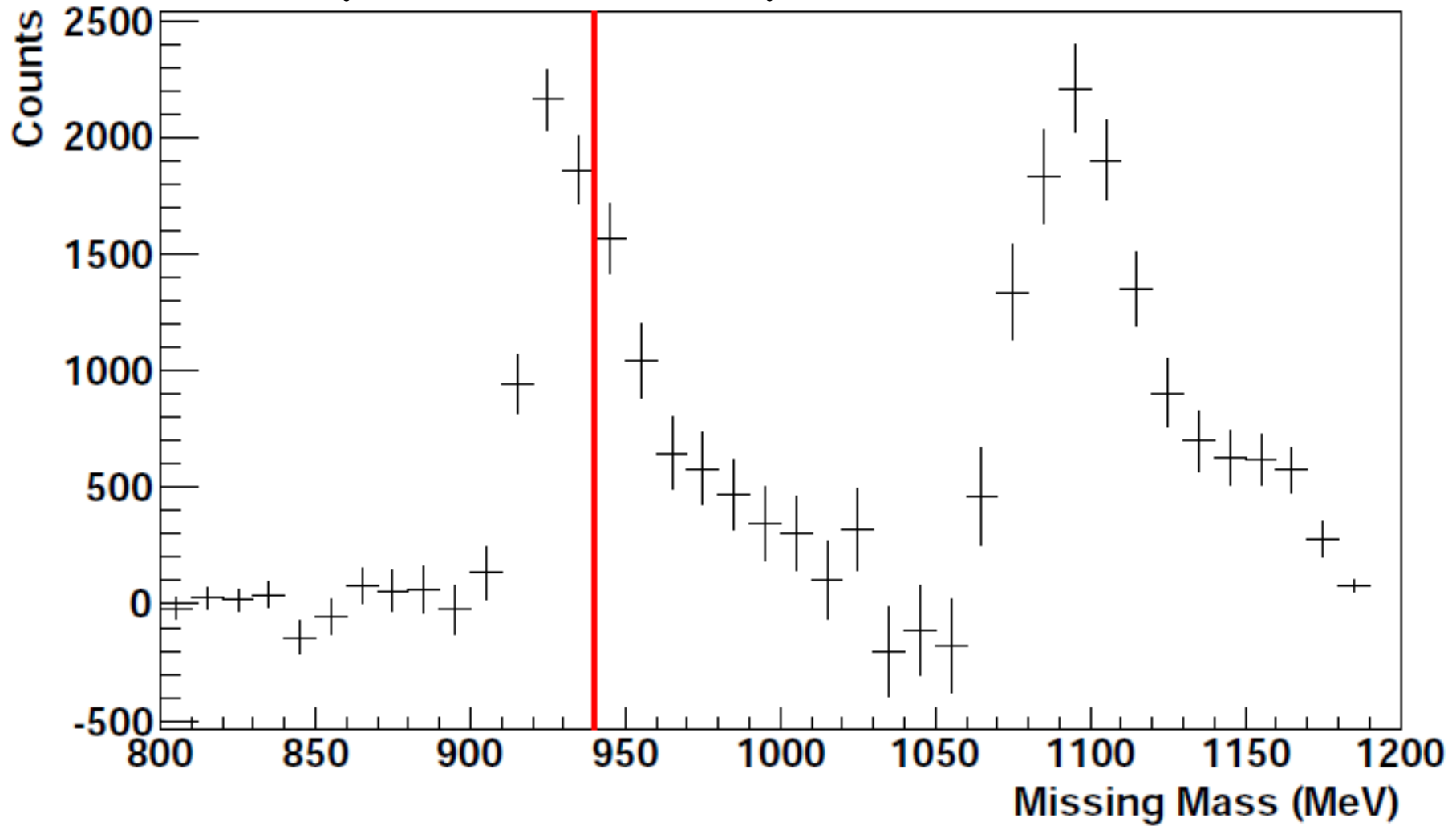
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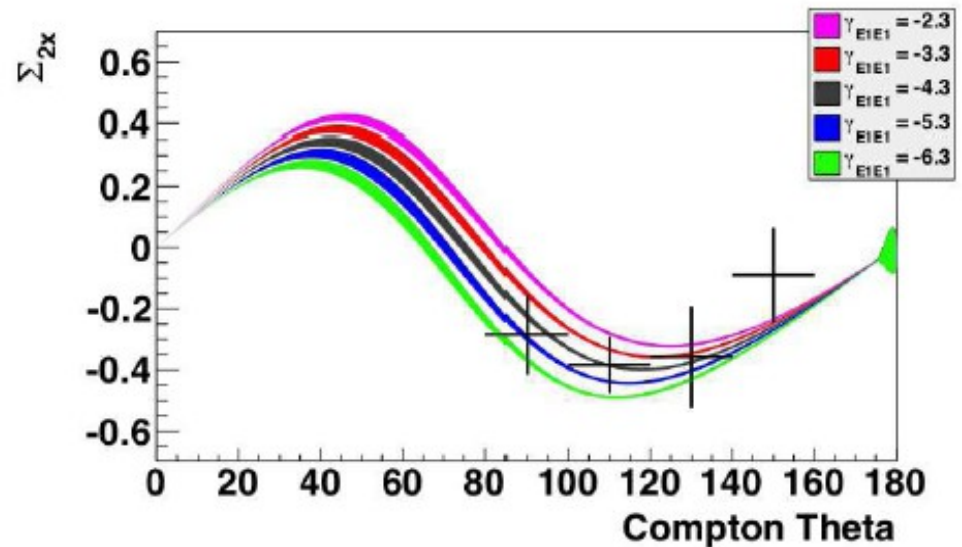
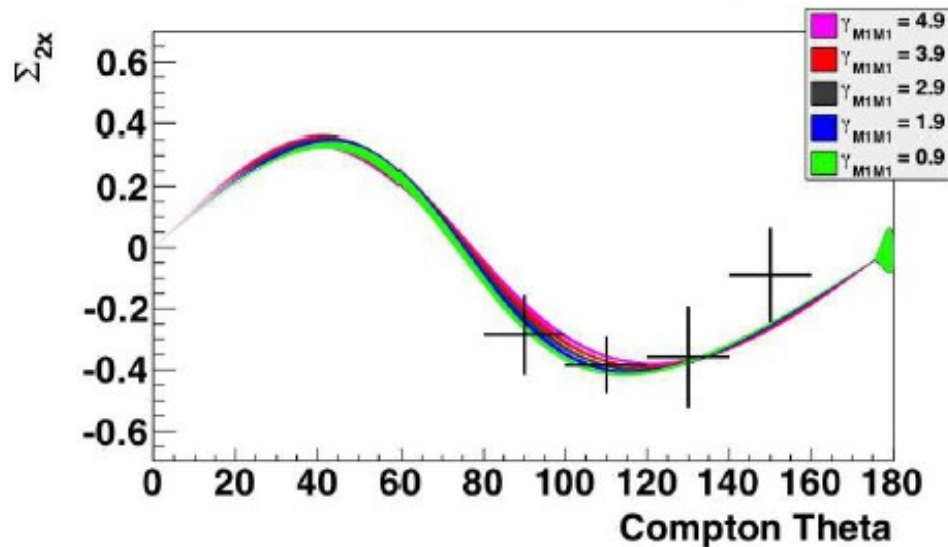
$E_\gamma = 273-303 \text{ MeV}$ ,  $\Theta_\gamma = 100-120^\circ$



**P. Martel (UMass, KPH Mainz)**

# $\Sigma_{2x}$ : Preliminary results

$$E_\gamma = 273 - 303 \text{ MeV}$$



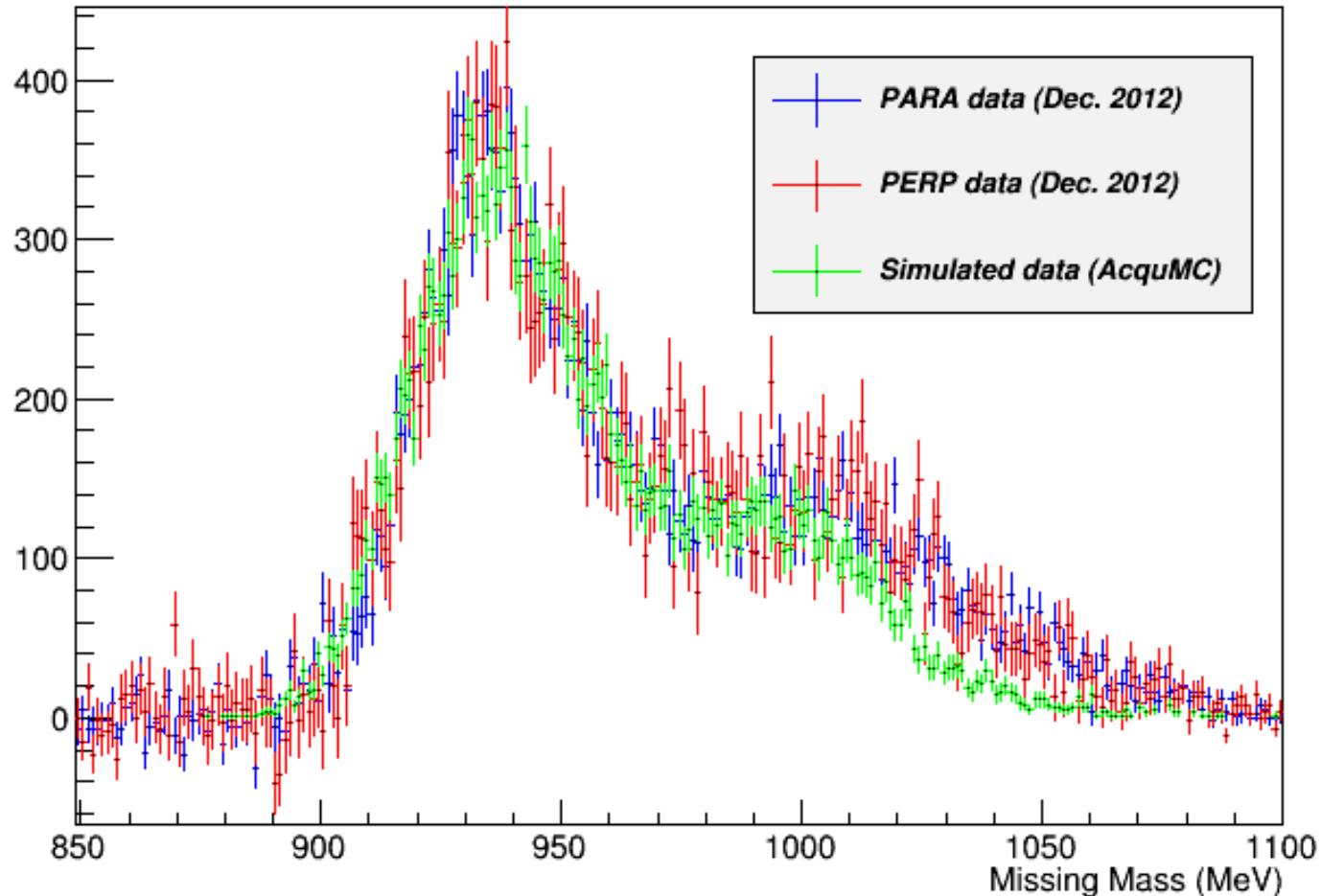
- First measurement of a double-polarized Compton scattering asymmetry on the nucleon,  $\Sigma_{2x}$
- Curves are from DR calculation of Pasquini et al. Data have sensitivity to the  $\gamma_{E1E1}$  spin-polarizability, with a preliminary estimate of

$$\gamma_{E1E1} = (-4.6 \pm 1.6) \times 10^{-4} \text{ fm}^4$$

P. Martel (UMass, KPH Mainz)

# Beam asymmetry $\Sigma_3$ at higher energies

## Missing mass comparison ( $E_\gamma = 270\text{-}290$ MeV)

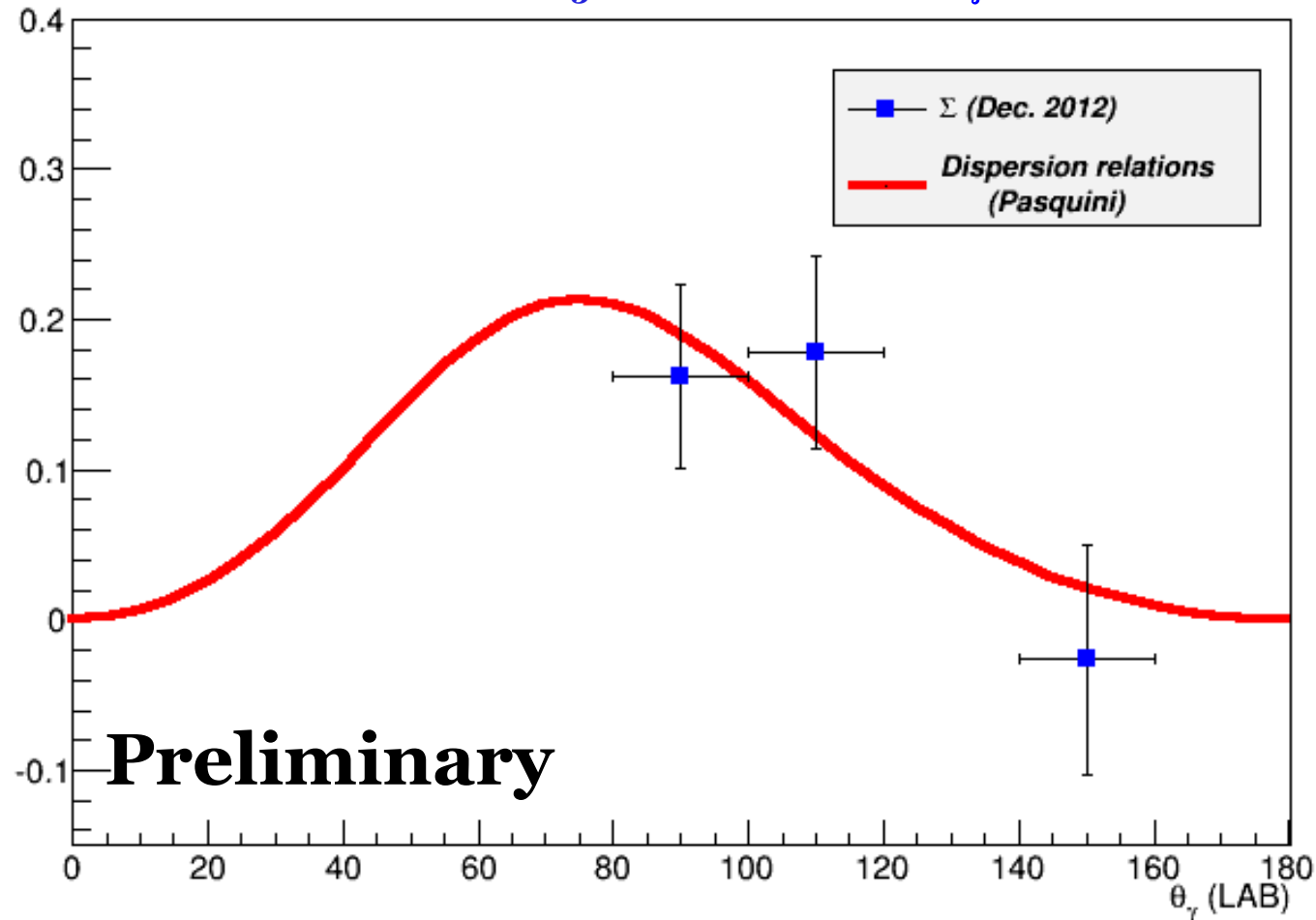


Simulated data includes both  $\gamma p \rightarrow \gamma p$  and  $\gamma p \rightarrow p\pi^0$

**C. Collicott (Mainz, DAL, SMU)**

# Beam asymmetry $\Sigma_3$ at higher energies

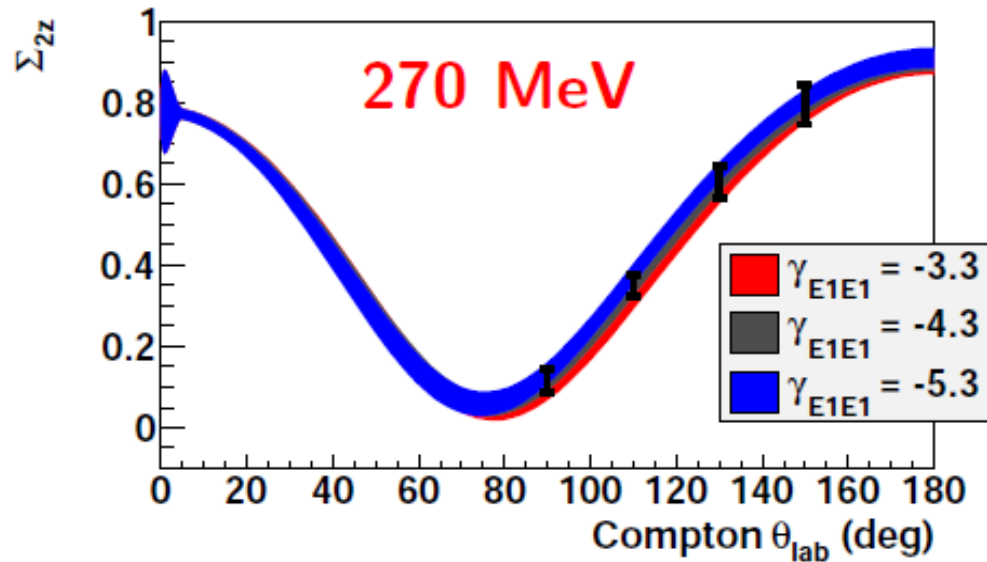
Compton scattering  $\Sigma_3$  asymmetry ( $E_\gamma = 270\text{-}290$  MeV)



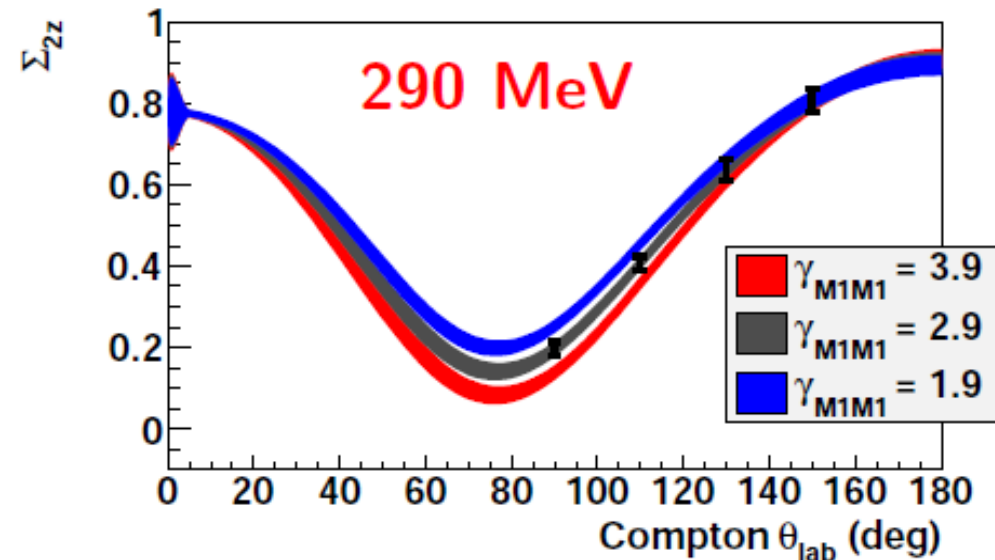
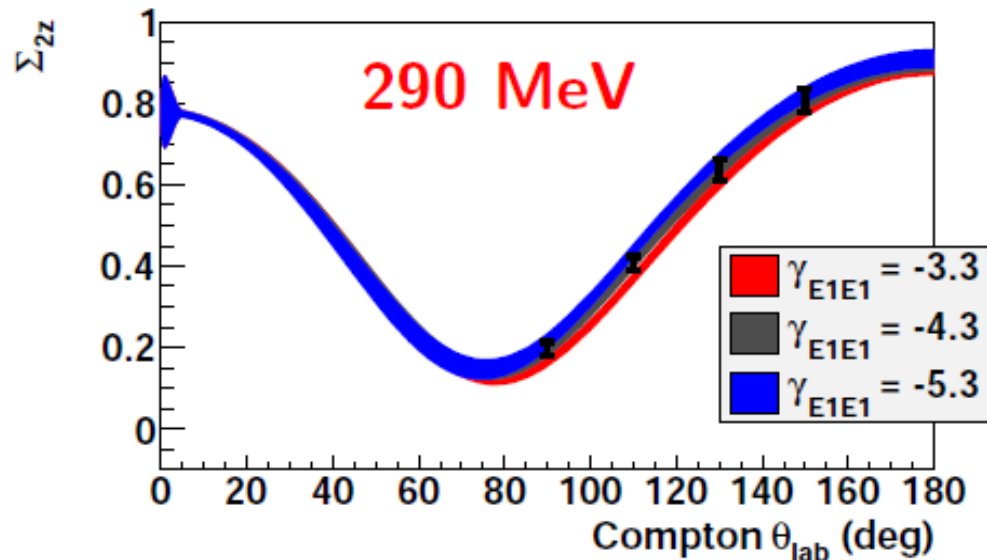
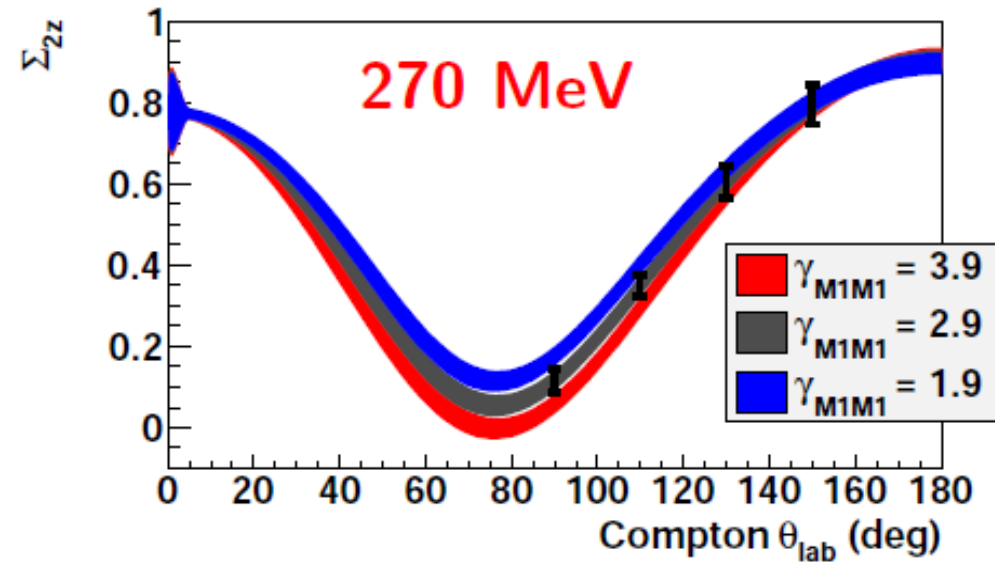
C. Collicott (Mainz, DAL, SMU)

# $\Sigma_{2Z}$ : Estimated experimental precision

Vary  $\gamma_{E1E1}$



Vary  $\gamma_{M1M1}$





# Current Status

Experiment	Status
$\Sigma_{2x}$	✓ February 2011
$\Sigma_3$ high energy	✓ December 2012
$\alpha, \beta (\Sigma_3 \text{ low energy})$	✓ June 2013
$\Sigma_{2z}$	May 2014

# Summary

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## Scalar polarizabilities:

- ◆ Events with signature of Compton scattering clearly identified
- ◆ Low-background data set obtained for the energy range 80-150 MeV
- ◆  $\Sigma_3$  measured below pion threshold for the first time, analysis in progress

## Spin polarizabilities:

- ◆ Double polarization observable  $\Sigma_{2x}$  measured for the first time in the  $\Delta$  region
- ◆ The asymmetries agree with a value of  $\gamma_{E_1E_1} = (-4.6 \pm 1.6) \times 10^{-4} \text{ fm}^4$
- ◆ Publication on  $\Sigma_{2x}$  in preparation (P.Martel et al.)
- ◆  $\Sigma_3$  measured in the  $\Delta$  region, analysis in progress (C. Collicott et al.)

# Outlook

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## Short-term:

- Finish analysis and publish  $\Sigma_{2x}$ ,  $\Sigma_3$ , and  $\alpha$ ,  $\beta$  results
- Measurement of  $\Sigma_{2z}$  will be performed in May (2014)
- Remeasure the observables  $\Sigma_3$ ,  $\Sigma_{2x}$  and  $\Sigma_{2z}$  with significantly higher statistics
- Complete extraction of the proton spin polarizabilities

## Medium and Long term:

- Development and installation of an active polarized target (prototype ready)
- Repeat the entire program on the neutron
- Installation of an active He gas target

# Outlook

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**Thank you for your attention!**

# Backup

# Real Compton Scattering – Hamiltonian

Expand the Hamiltonian in incident-photon energy.

0th order  $\longrightarrow$  charge, mass

1st order  $\longrightarrow$  magnetic moment

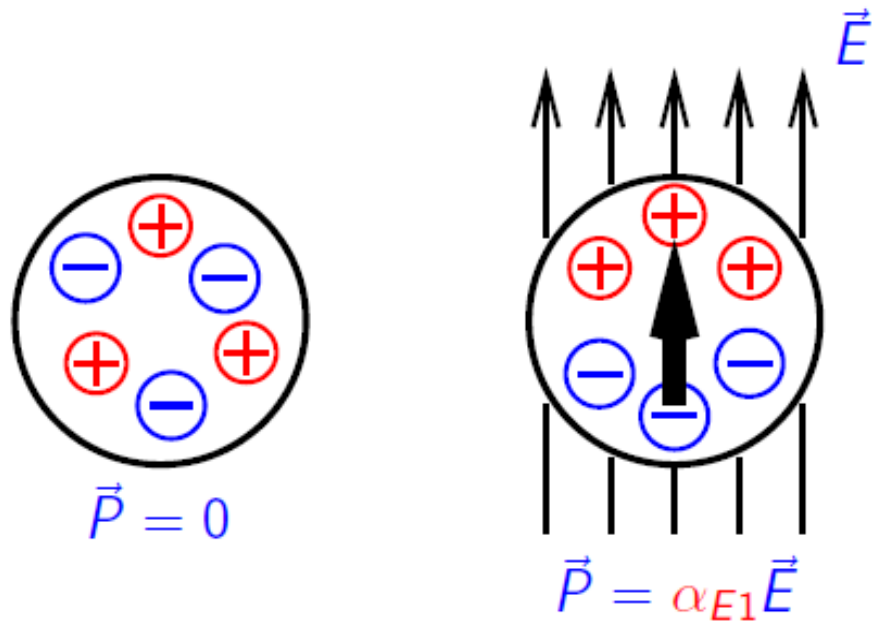
2nd order  $\longrightarrow$  **scalar polarizabilities:**

$$H_{\text{eff}}^{(2)} = -4\pi \left[ \frac{1}{2} \alpha_{E1} \vec{E}^2 + \frac{1}{2} \beta_{M1} \vec{H}^2 \right]$$

3rd order  $\longrightarrow$  **spin (or vector) polarizabilities:**

$$H_{\text{eff}}^{(3)} = -4\pi \left[ \frac{1}{2} \gamma_{E1E1} \vec{\sigma} \cdot (\vec{E} \times \dot{\vec{E}}) + \frac{1}{2} \gamma_{M1M1} \vec{\sigma} \cdot (\vec{H} \times \dot{\vec{H}}) \right. \\ \left. - \gamma_{M1E2} E_{ij} \sigma_i H_j + \gamma_{E1M2} H_{ij} \sigma_i E_j \right]$$

## Electric Dipole Polarizability

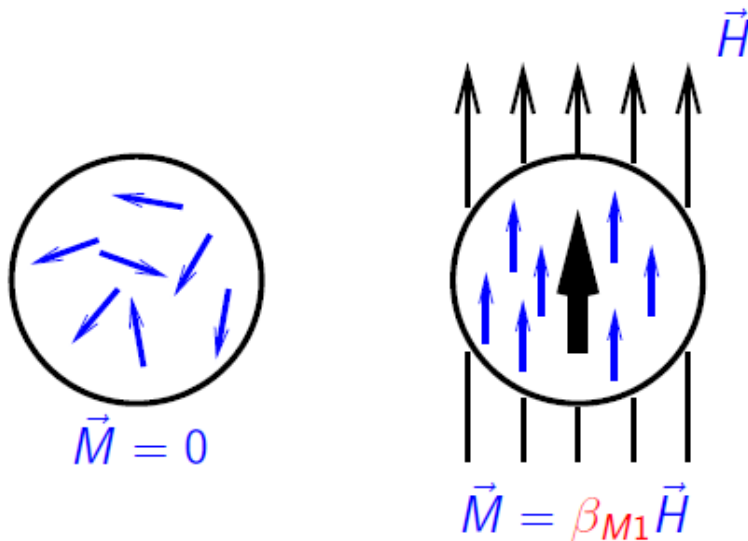


- ▶ Apply an electric field to a composite system
- ▶ Separation of Charge, or **“Stretchability”**
- ▶ Proportionality constant between electric dipole moment and electric field is the electric dipole polarizability,  $\alpha_{E1}$ .

Provides information on force holding system together.

# Scalar Polarizabilities – Conceptual

## Magnetic Dipole Polarizability



- ▶ Apply a magnetic field to a composite system
- ▶ Alignment of dipoles or **“Alignability”**
- ▶ Proportionality constant between magnetic dipole moment and magnetic field is the magnetic dipole polarizability,  $\beta_{M1}$ .
- ▶ Two contributions, paramagnetic and diamagnetic, and they cancel partially, giving  $\beta_{M1} < \alpha_{E1}$ .

Provides information on force holding system together.



## Previous Data – $\gamma_0$

Forward spin polarizability has been determined by a “GDH-type” of sum rule

$$\begin{aligned}\gamma_0 &= -\gamma_{E1E1} - \gamma_{M1M1} - \gamma_{E1M2} - \gamma_{M1E2} \\ &= -\frac{1}{4\pi^2} \int_{\nu_{\text{thr}}}^{\infty} \frac{\sigma_{3/2}(\nu) - \sigma_{1/2}(\nu)}{\nu^3} d\nu \\ &= (-1.00 \pm 0.08 \pm 0.10) \times 10^{-4} \text{ fm}^4\end{aligned}$$

Known to  $\approx 10\%$ .

## Previous Data – $\gamma_\pi$

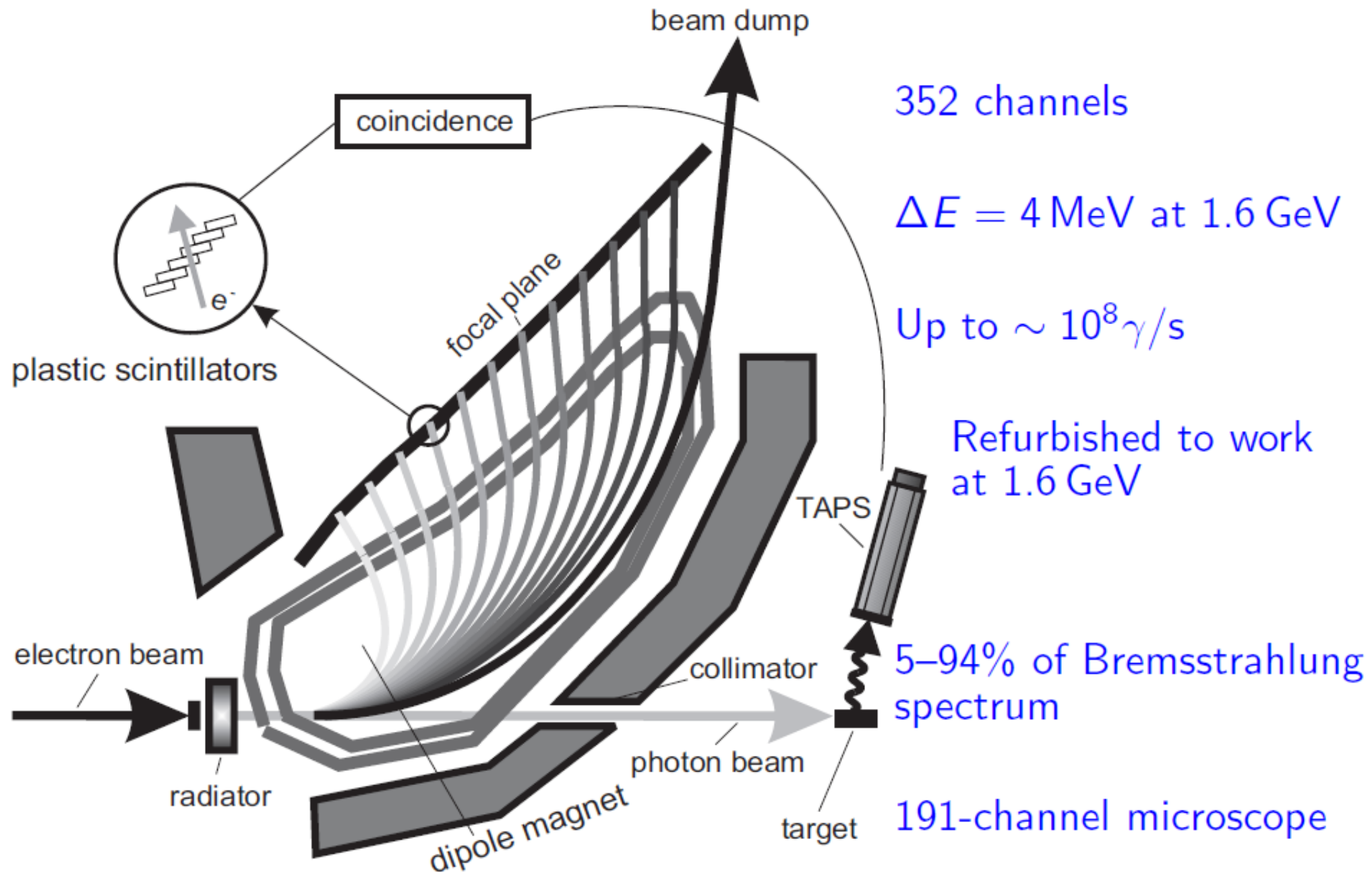
Backward spin polarizability has been determined from a dispersive analysis of backward-angle Compton scattering

$$\begin{aligned}\gamma_\pi &= -\gamma_{E1E1} + \gamma_{M1M1} - \gamma_{E1M2} + \gamma_{M1E2} \\ &= (-38.7 \pm 1.8) \times 10^{-4} \text{ fm}^4\end{aligned}$$

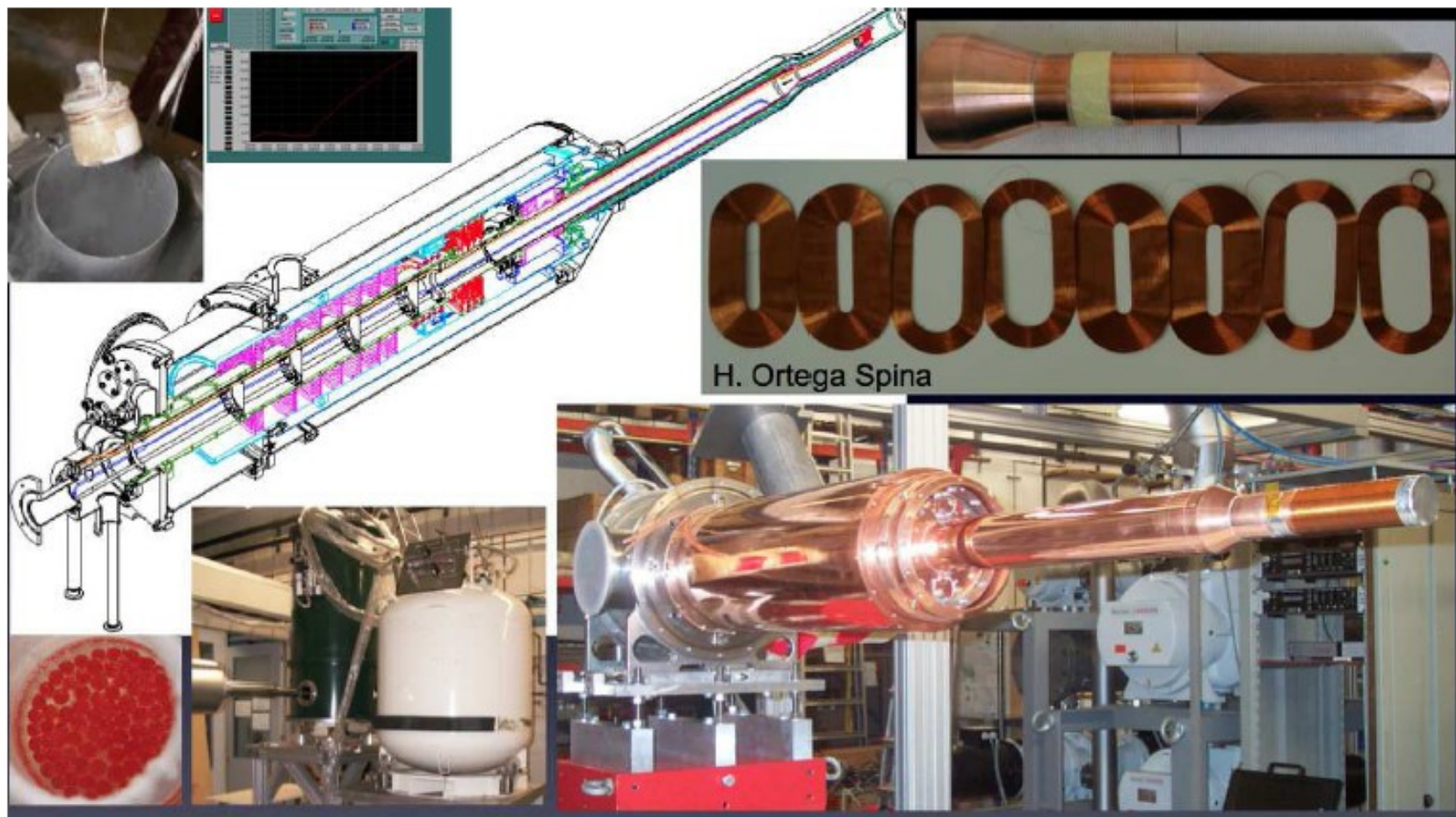
where the pion pole contributes  $-46.7$  and the dispersive part  $8.0 \pm 1.8$ .

Note that the dispersive part is known *only* to about  $\approx 25\%$ !

# Incident Photon Beam – Glasgow-Mainz Photon Tagger



# Polarized Target



Dynamical Nucleon Polarization

Target material is butanol,  $\text{C}_4\text{H}_{10}\text{O}$

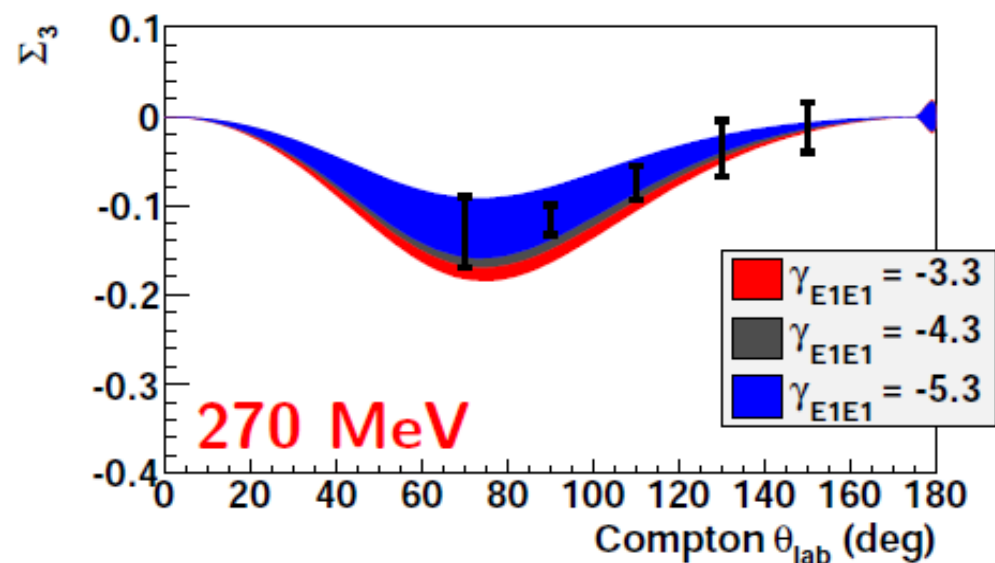
Dilution cryostat with bath of liquid  $^3\text{He}/^4\text{He}$ ,  $T < 30 \text{ mK}$

$P_p \approx 90\%$  with a relaxation time of  $\tau > 1000 \text{ hours}$ .

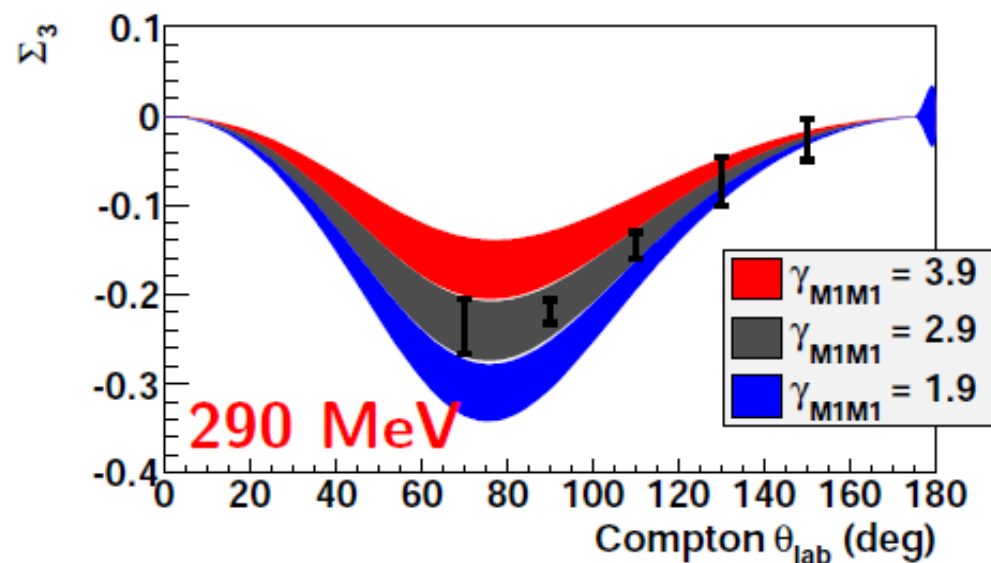
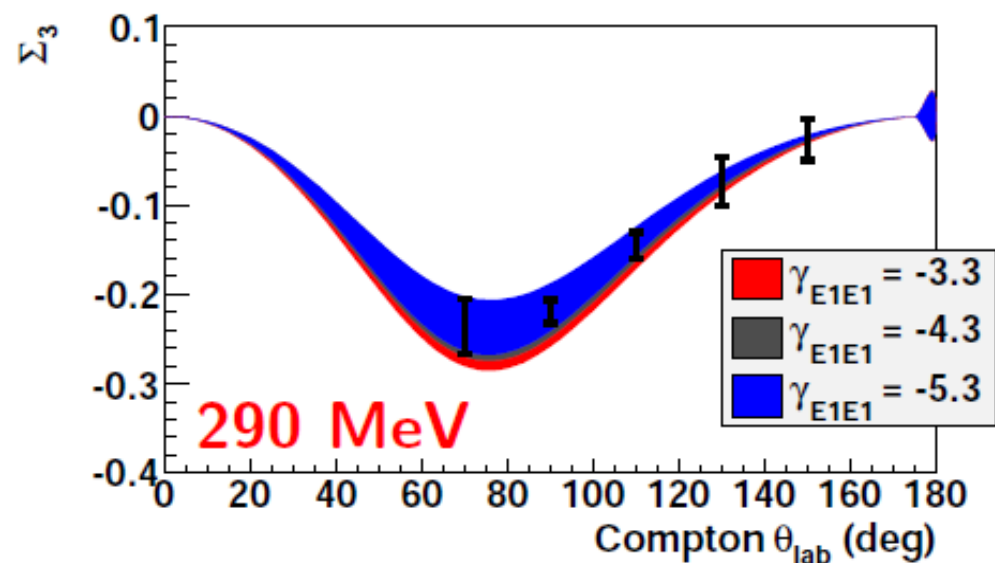
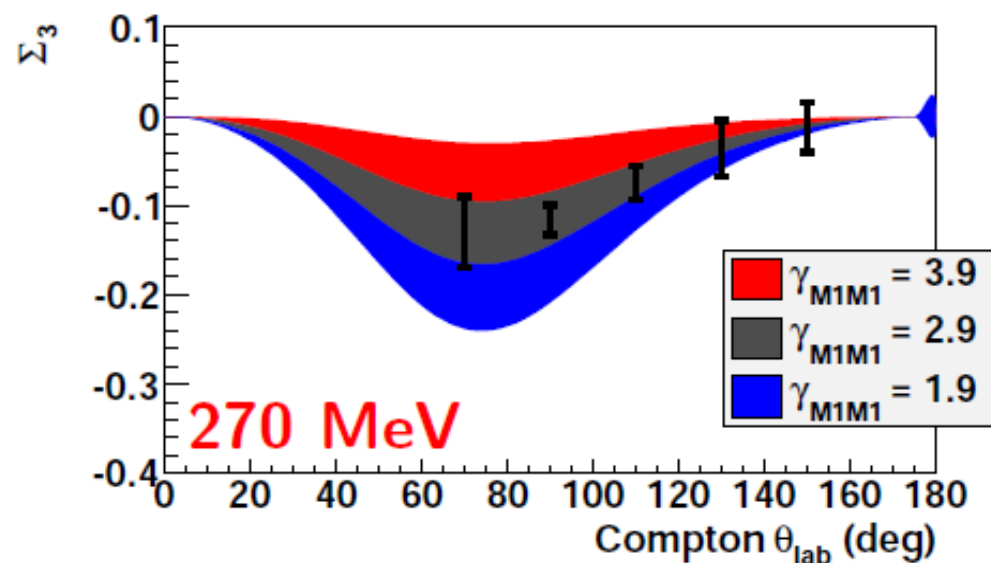


# $\Sigma_3$ – Estimated Experimental Precision

Vary  $\gamma_{E1E1}$



Vary  $\gamma_{M1M1}$



# Predicted Values

Extracting the proton spin polarizabilities would provide a useful test of nucleon structure.

	$O(p^3)$	$O(p^4)$	$O(p^4)$	LC3	LC4	SSE	BGLMN	HDPV	KS
$\gamma_{E1}$	-5.7	-1.4	-1.8	-3.2	-2.8	-5.7	-3.4	-4.3	-5.0
$\gamma_{M2}$	1.1	0.2	0.7	0.7	0.8	.98	0.3	-0.01	-1.8
$\gamma_{E2}$	1.1	1.8	1.8	0.7	0.3	.98	1.9	2.1	1.1
$\gamma_{M1}$	-1.1	3.3	2.9	-1.4	-3.1	3.1	2.7	2.9	3.4
$\gamma_0$	4.6	-3.9	-3.6	3.1	4.8	.64	-1.5	-0.7	2.3
$\gamma_\pi$	4.6	6.3	5.8	1.8	-0.8	8.8	7.7	9.3	11.3

**Table:** Values for the spin polarizabilities.  $O(p^n)$  are Chiral Perturbation Theory (ChPT) calculations. LC3 and LC4 are  $O(p^3)$  and  $O(p^4)$  Lorentz invariant ChPT calculations, respectively. SSE is a Small Scale Expansion calculation. The remaining three are all dispersion relation calculations.

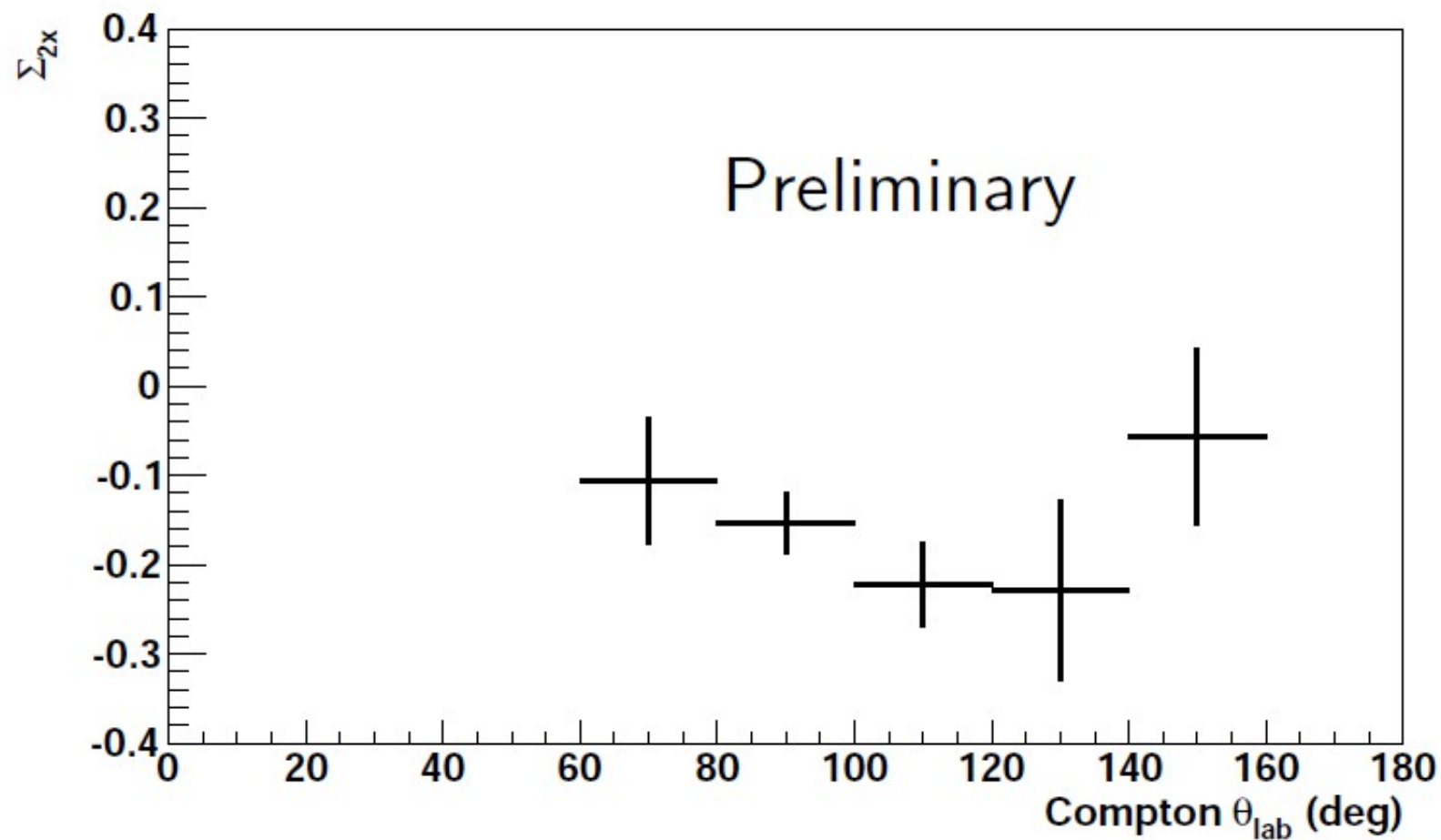
# Frozen Spin Target

Polarizing protons through Dynamic Nuclear Polarization (DNP):

- Cool target to 0.2 Kelvin.
- Use 2.5 Tesla magnet to align electron spins.
- Pump  $\approx 70$  GHz microwaves (just above, or below, the Electron Spin Resonance frequency), causing spin-flips between the electrons and protons.
- Cool target to 0.025 Kelvin, 'freezing' proton spins in place.
- Remove polarizing magnet.
- Energize 0.6 Tesla 'holding' coil in the cryostat to maintain the polarization.
- Relaxation times  $> 1000$  hours.
- Polarizations up to 90%.



# Transverse Asymmetries - $E_\gamma=315\text{-}346$ MeV



Above validity of dispersion relation.





# Compton scattering: Polarisabilities

The polarisabilities can be defined in terms of the angular momentum and parity of the incident and scattered photon.

A photon with total angular momentum  $L$ , is said to be electric (EL) or magnetic (ML) if its parity satisfies:

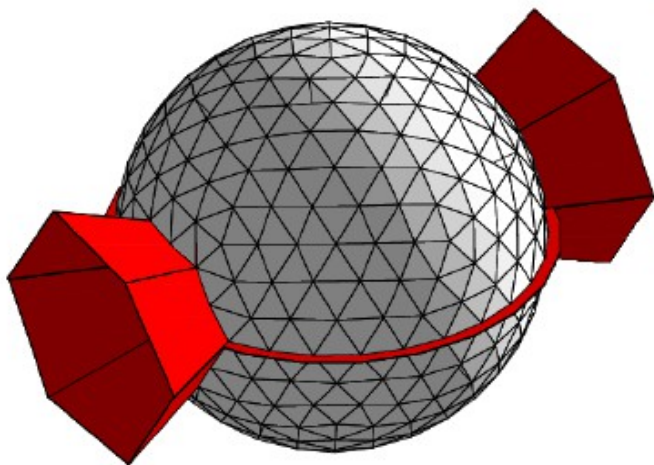
$$\pi_{EL} = (-1)^L \quad \pi_{ML} = (-1)^{L+1}$$

The  $\gamma_{M1E2}$  polarisability, for example, can now be described in terms of the incoming and outgoing photon properties. In this case, the incoming and outgoing photons carry total angular momentum and parity given by  $2^+$  and  $1^+$  respectively.

# Crystal Ball

The CB is a highly segmented NaI(Tl) detector (composed of 672 individual crystals) which surrounds the MWPCs, PID and target.

- There are two gaps in the CB (beam entrance/exit) which results in an angular coverage for the CB system (CB, MWPCs, and PID) of ( $\theta = 20^\circ \rightarrow 160^\circ$ ) and ( $\phi = 0^\circ \rightarrow 180^\circ$ )



- The huge CB angular coverage is ideal for Compton scattering experiments to suppress the huge  $\pi^0$  background!
- Excellent photon detection:  
 $\sigma_E \approx 4\%$     $\sigma_\theta \approx 2^\circ$     $\sigma_\phi \approx \frac{2^\circ}{\sin \theta}$   
(better than crystal size!).

Low Energy Expansion for parallel polarization:

$$\frac{d\sigma^{\parallel}}{d\Omega} = \frac{d\sigma^{\parallel}}{d\Omega}_{\text{Born}} - \frac{e^2}{2m} \left( \frac{\nu'}{\nu} \right)^2 \nu\nu' (\alpha_{E1} z^2 + \beta_{M1} z) + O(\nu^3)$$

Low Energy Expansion for perpendicular polarization:

$$\frac{d\sigma^{\perp}}{d\Omega} = \frac{d\sigma^{\perp}}{d\Omega}_{\text{Born}} - \frac{e^2}{2m} \left( \frac{\nu'}{\nu} \right)^2 \nu\nu' (\alpha_{E1} + \beta_{M1} z) + O(\nu^3)$$

Difference: dependent purely on  $\alpha$ :

$$\frac{d\sigma^{\perp} - d\sigma^{\parallel}}{d\Omega} = \left( \frac{d\sigma^{\perp} - d\sigma^{\parallel}}{d\Omega} \right)_{\text{Born}} - \frac{e^2}{2m} \left( \frac{\nu'}{\nu} \right)^2 \nu\nu' \alpha_{E1} (1 - z^2) + O(\nu^3)$$

Difference multiplied by  $z^2 = \cos^2(\theta)$ : dependent purely on  $\beta$ :

$$\frac{z^2 d\sigma^{\perp} - d\sigma^{\parallel}}{d\Omega} = \left( \frac{z^2 d\sigma^{\perp} - d\sigma^{\parallel}}{d\Omega} \right)_{\text{Born}} - \frac{e^2}{2m} \left( \frac{\nu'}{\nu} \right)^2 \nu\nu' \beta_{M1} z (z^2 - 1) + O(\nu^3)$$

Low Energy Expansion: limited validity, dependence similar to ChPT

# General information

## Standard A2 Equipment is required:

- MAMI electrons
- Glasgow-Mainz Tagger
- CB-TAPS detector system
- Cryogenic Targets

Run Parameter	$\Sigma_{2x}/\Sigma_{2z}$	$\Sigma_3$ and $\alpha_{E1}, \beta_{M1}$
Electron Beam Energy	450 MeV	883 MeV
Target	butanol	LH <sub>2</sub>
Radiator	Copper	Diamond
Tagged Energy Range	100 – 400 MeV	100 – 400 MeV
Channel Energy Resolution	1 MeV	2 MeV
Beam Polarization	circular	linear
Target Polarization	transverse/longitudinal	none



# Beam asymmetry $\Sigma_3$ : existing data

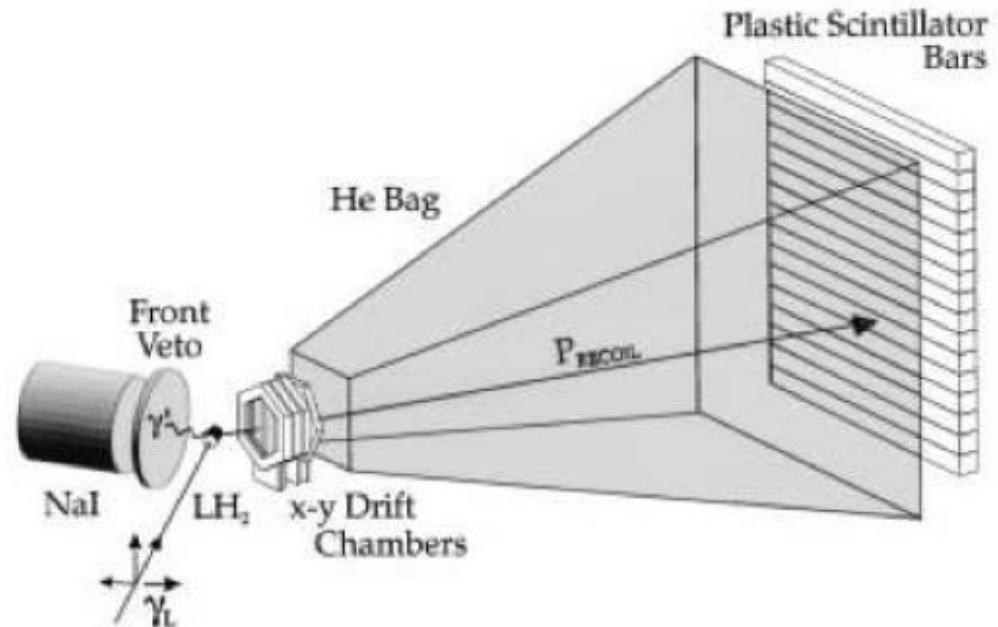
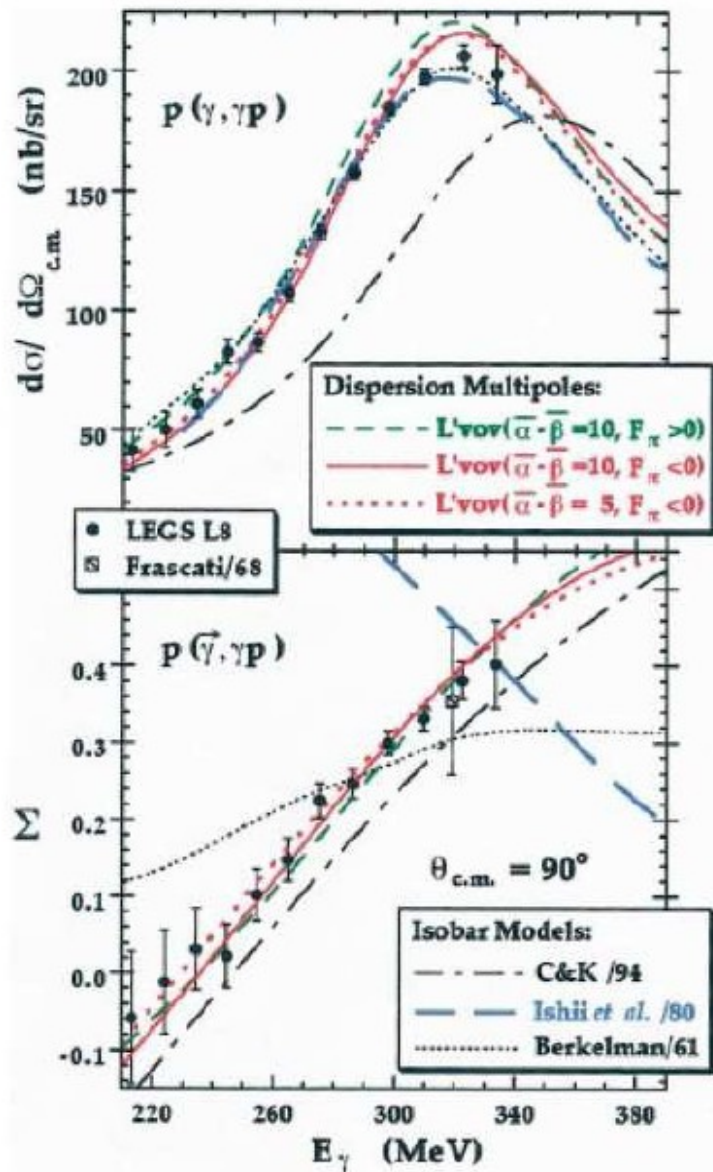
LEGS

$$\vec{\gamma}p \rightarrow \gamma p$$

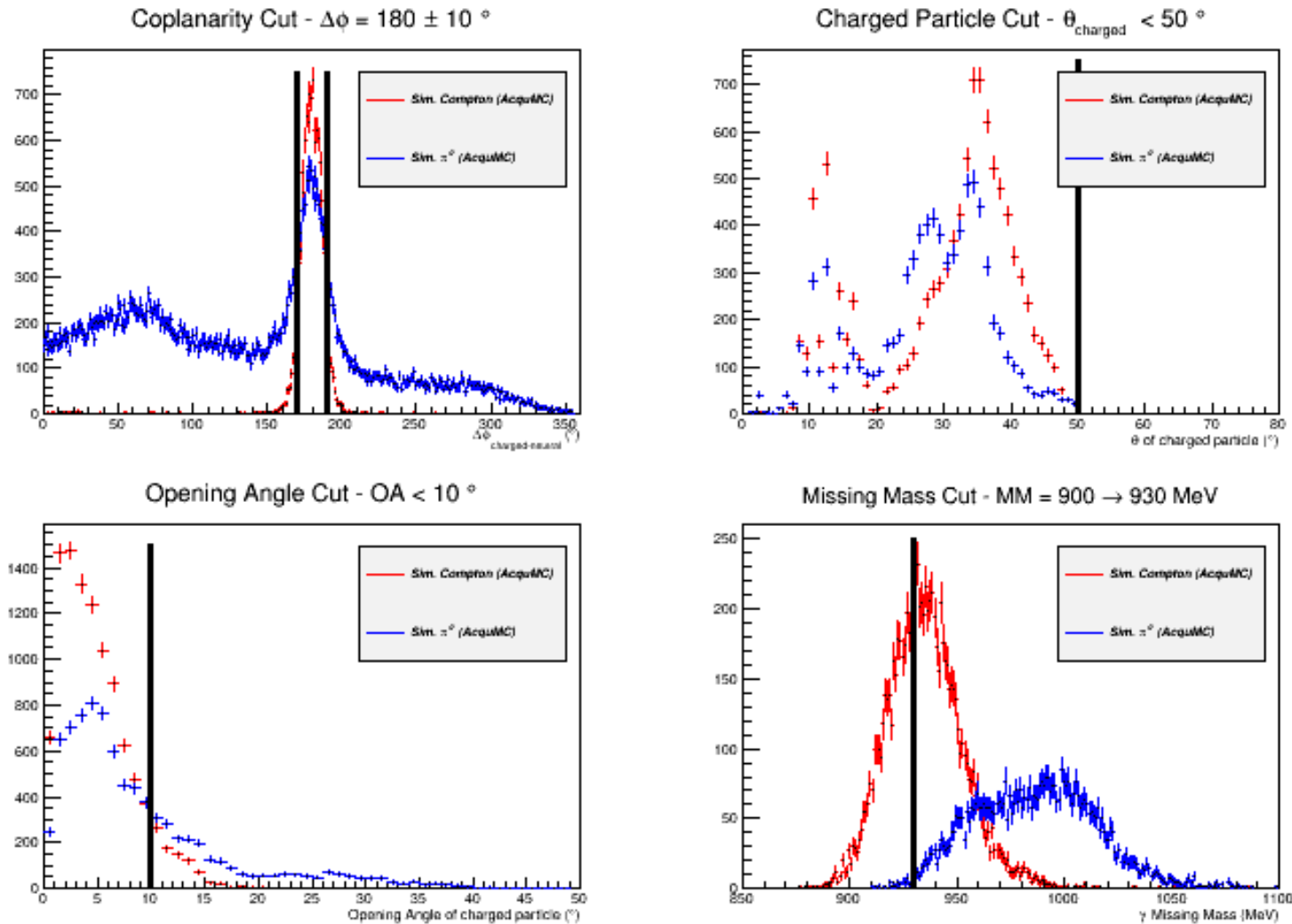
$d\sigma/d\Omega$  and  $\Sigma_3$

$$E_\gamma = 200 - 350 \text{ MeV}$$

$$\theta_{\gamma'} = 90^\circ \text{ ONLY!}$$

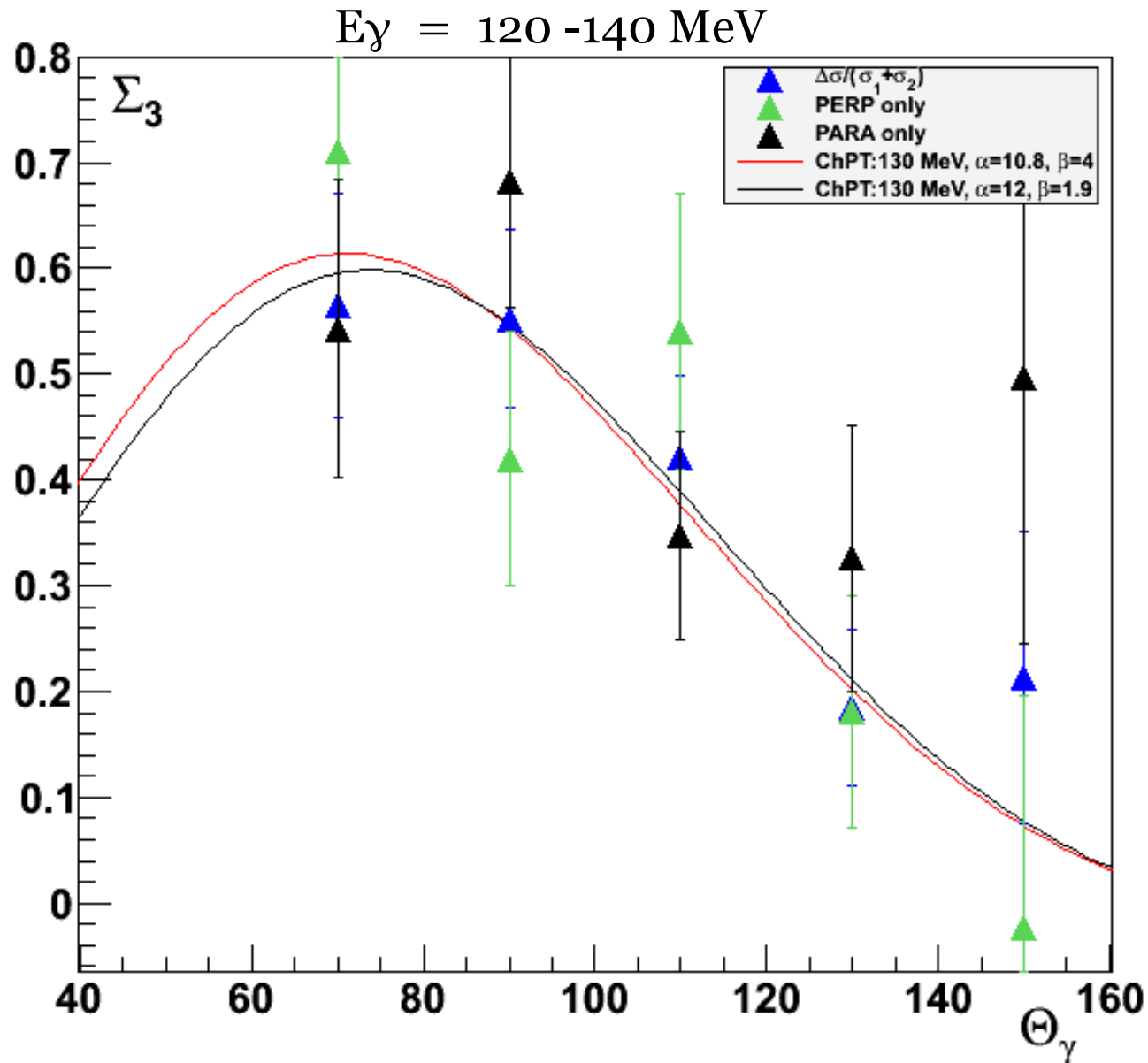


# Beam asymmetry $\Sigma_3$ at higher energies



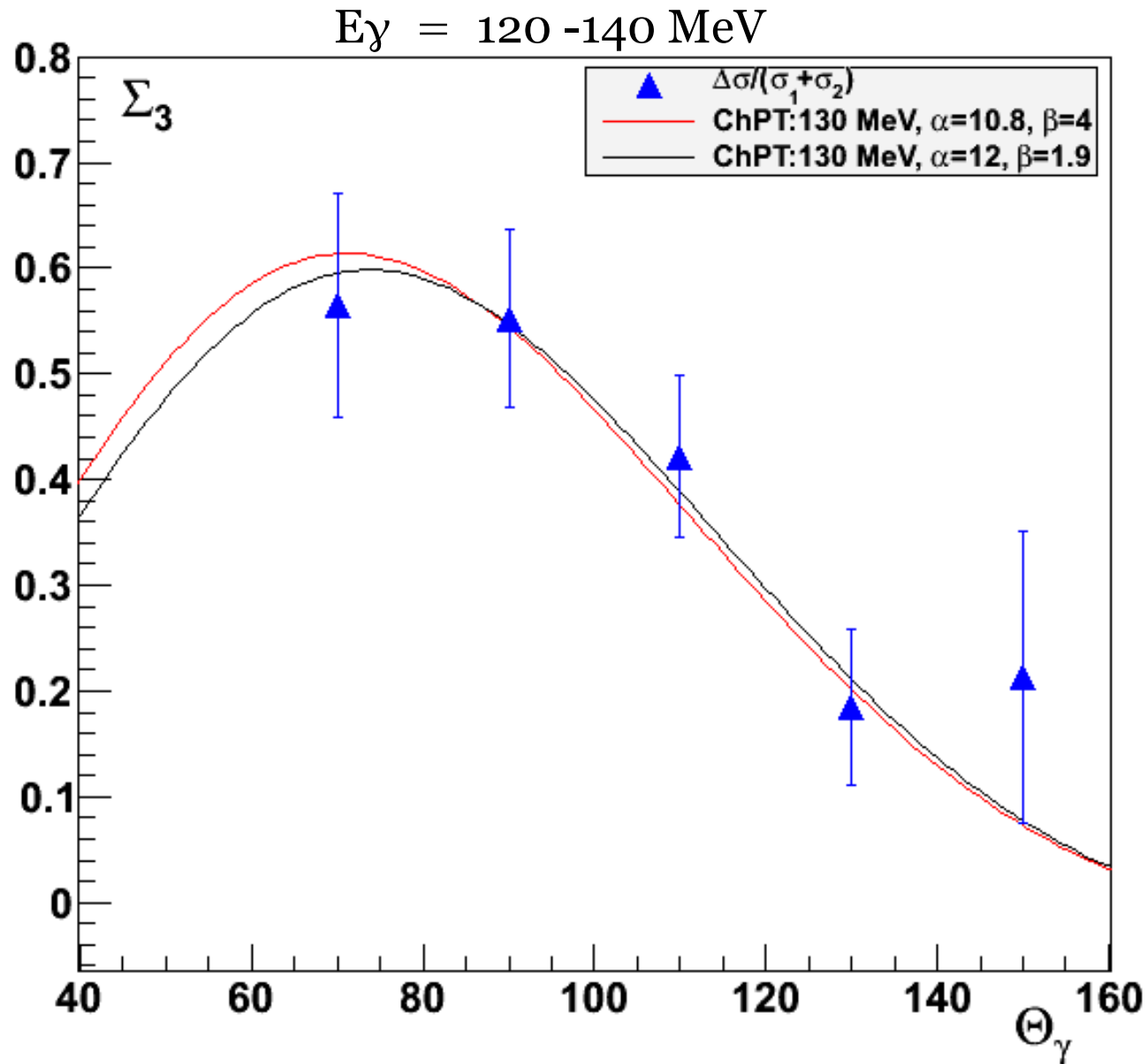
C. Collicott (Mainz, DAL, SMU)

# Beam asymmetry $\Sigma_3$ : systematic cross-checks



Very  
Preliminary

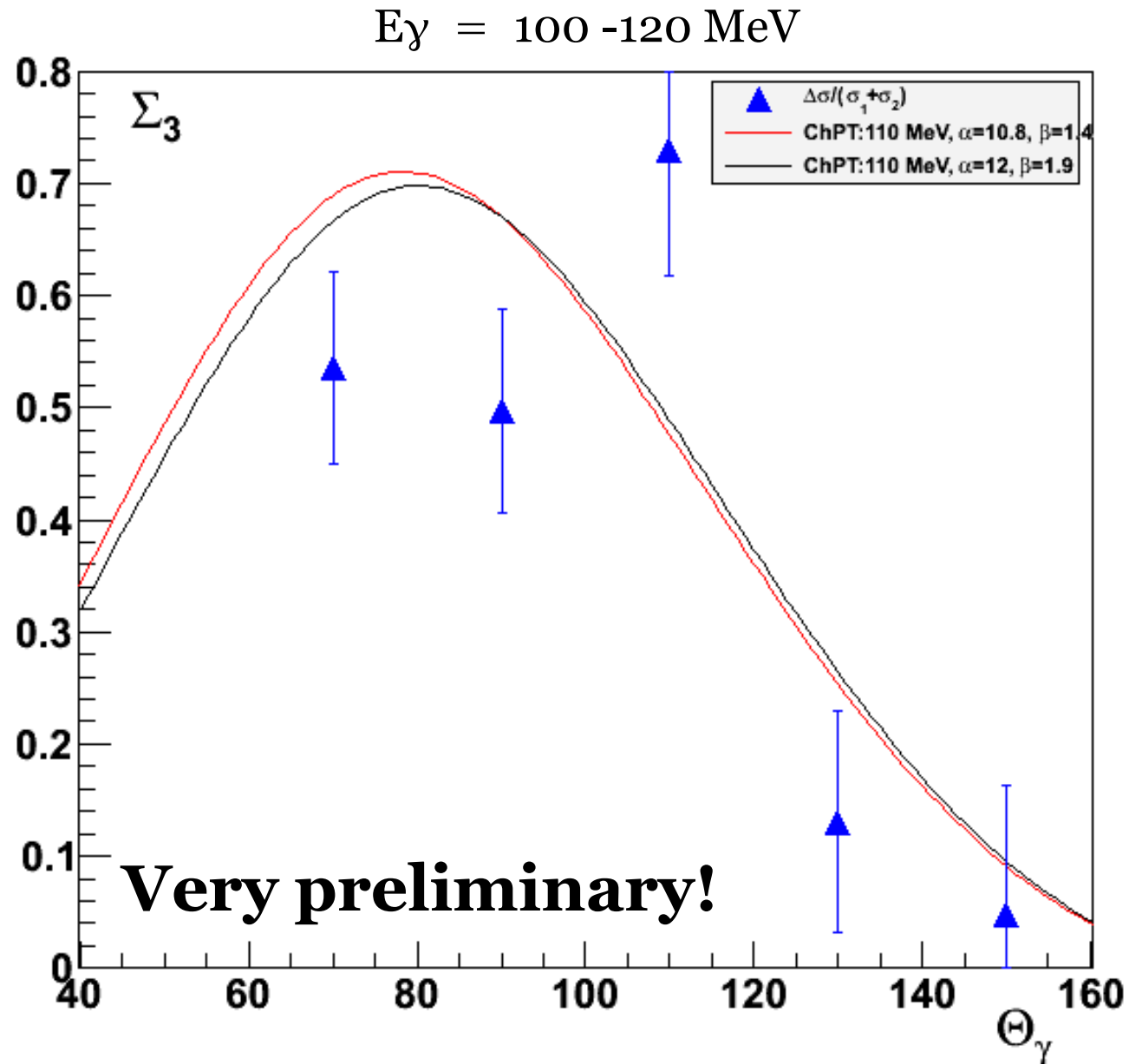
# Beam asymmetry $\Sigma_3$ : Preliminary results



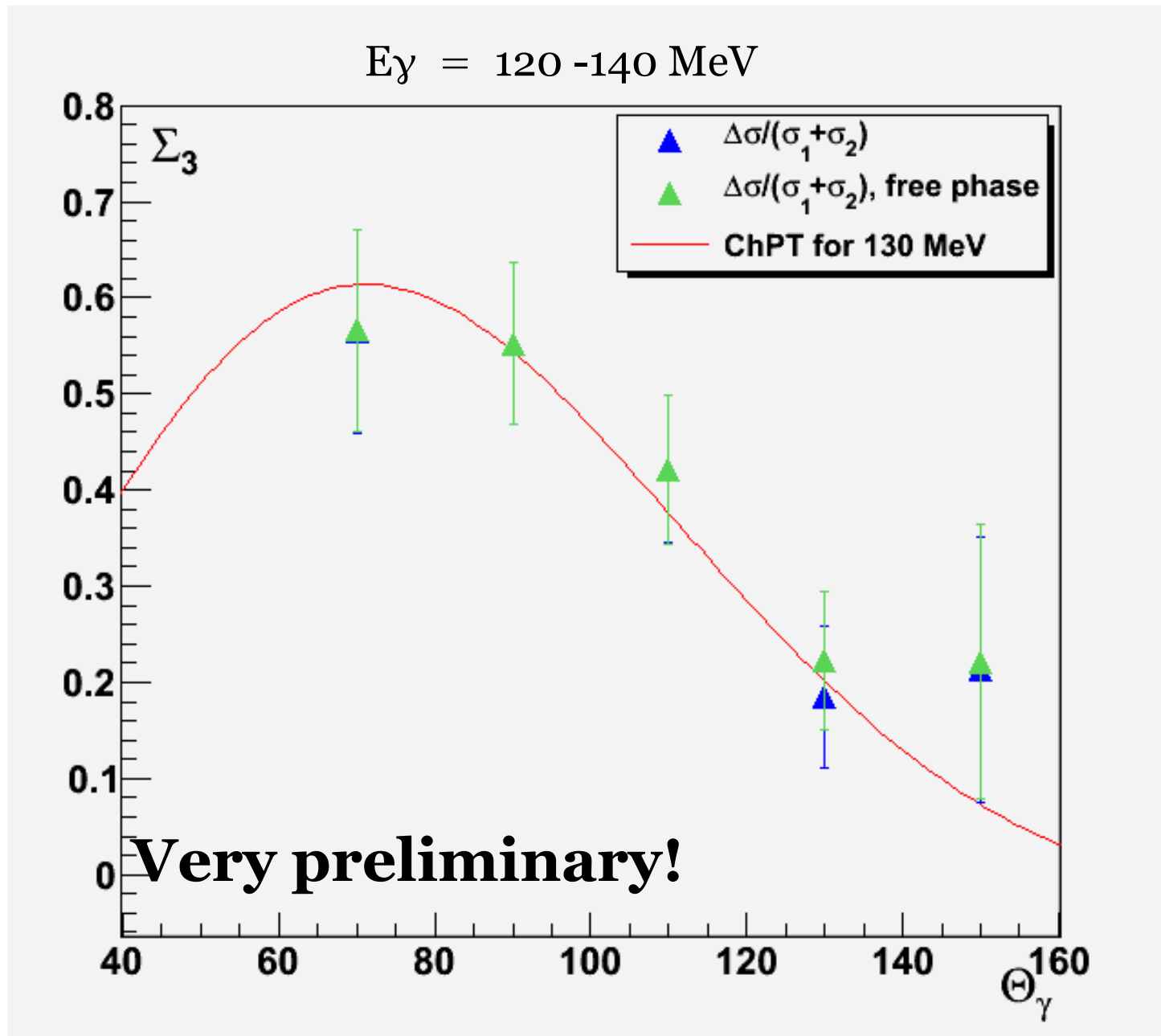
Very  
Preliminary



# Beam asymmetry $\Sigma_3$ : Preliminary results

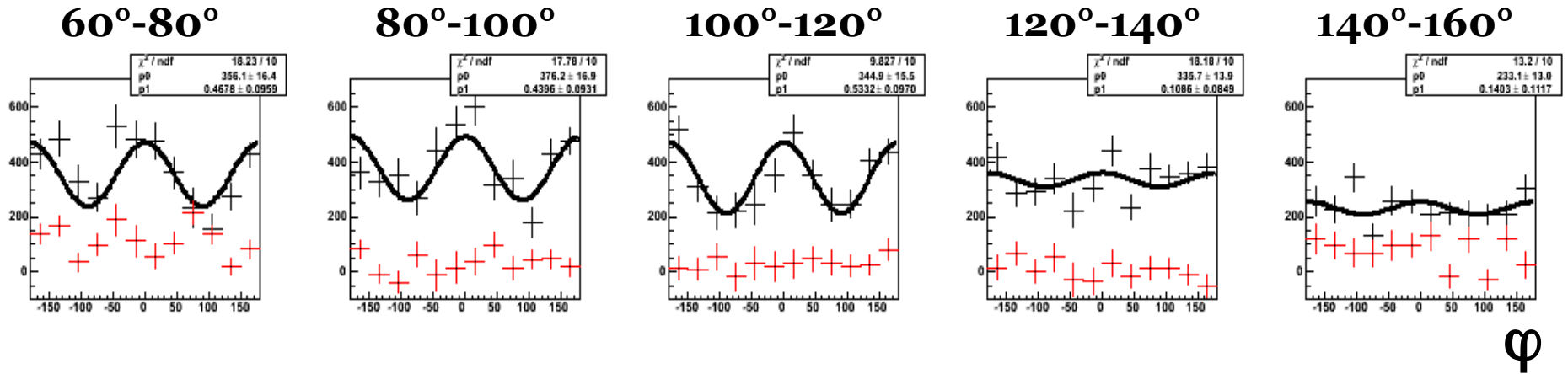


# Beam asymmetry $\Sigma_3$ : Preliminary results



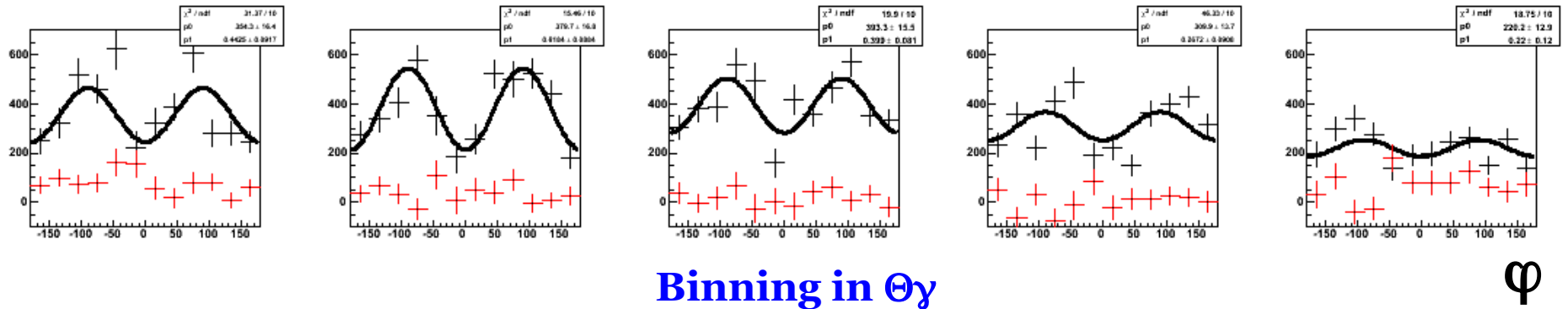
# $\varphi$ – full and empty target contributions

PERP



$\varphi$

PARA



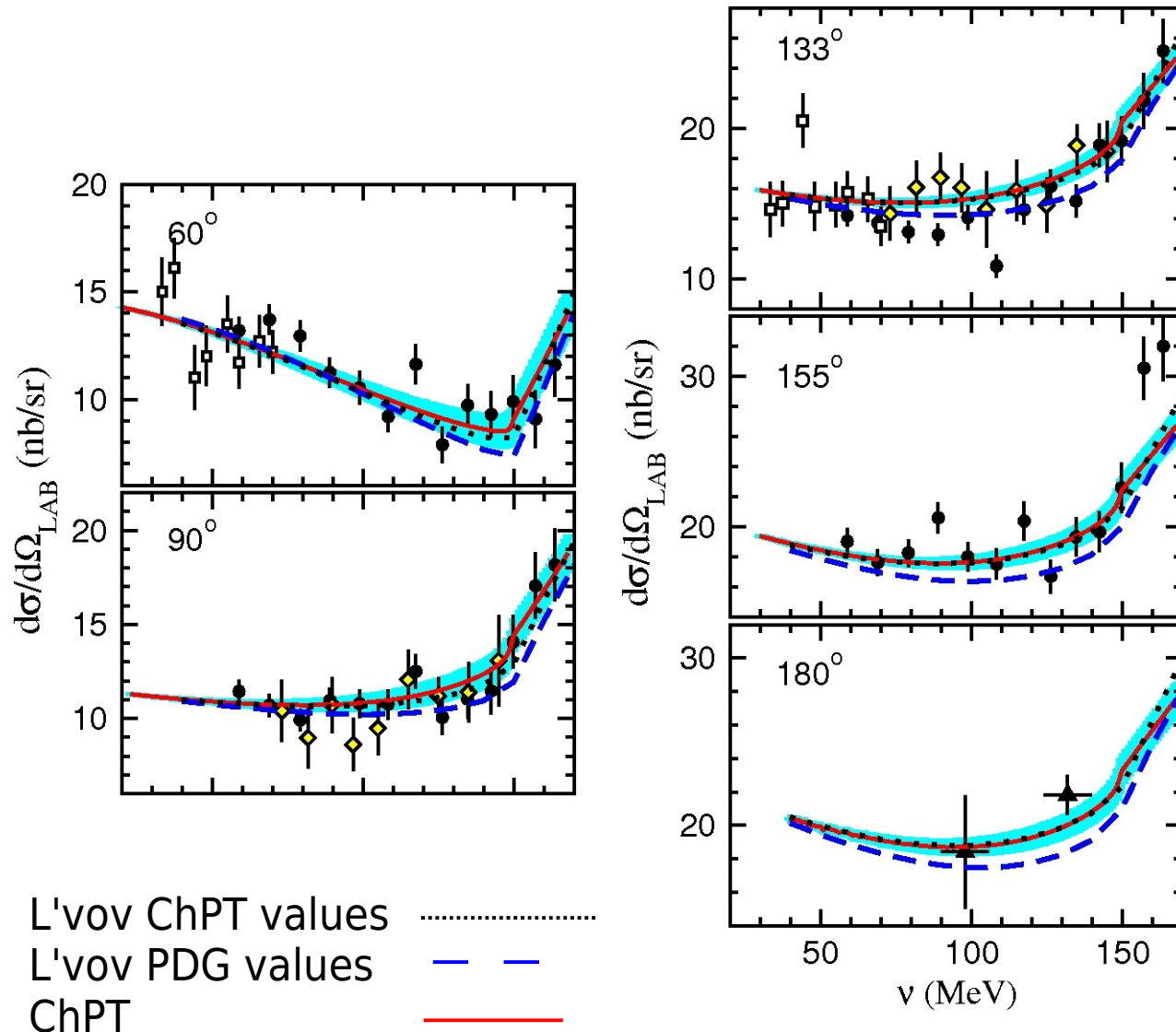
$\varphi$

Binning in  $\Theta_Y$

Preliminary

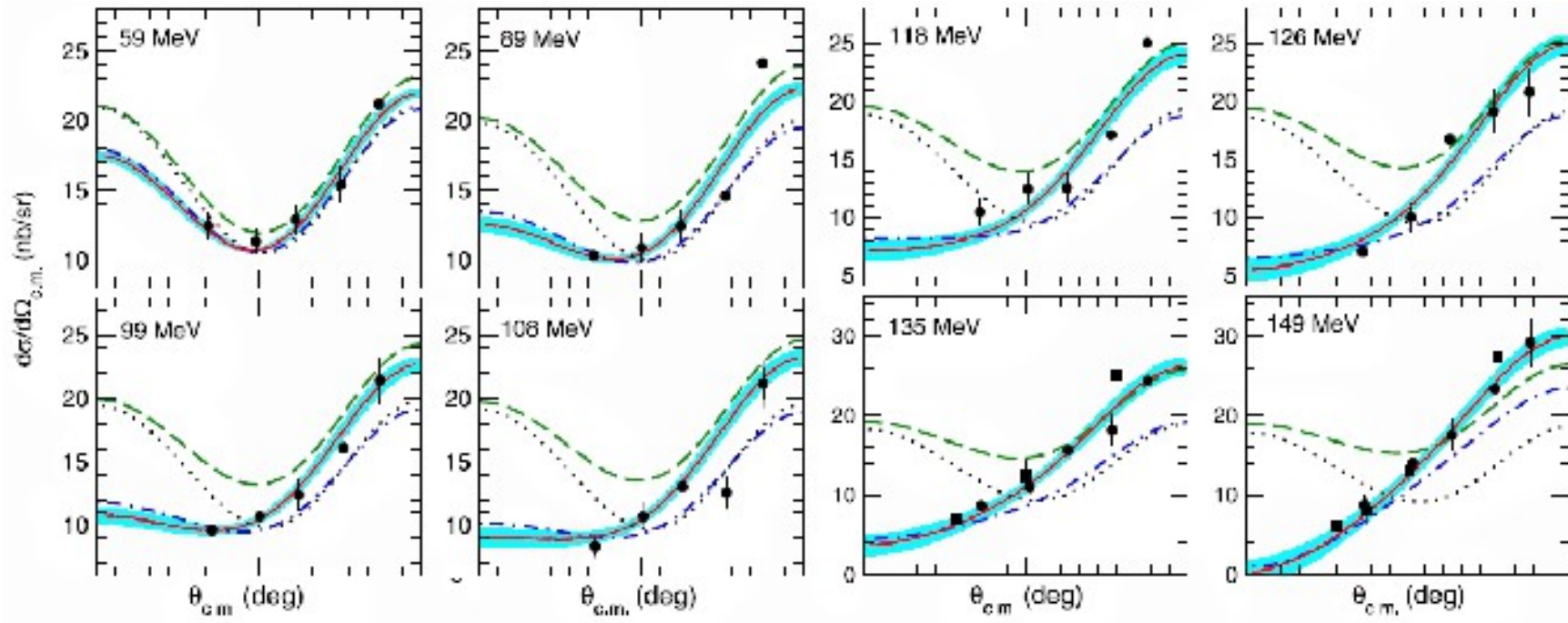
# Existing data and model predictions

## Agreement between Pascalutsa (ChPT) and L'vov (Dispersion Relations)



Squares: Illinois,  
F. J. Federspeil et al. Phys. Rev. Lett. **67** 1511 (1991)  
Triangles: MAMI,  
A. Zieger et al. Phys. Lett. B **278** 34 (1992)  
Diamonds: SAL,  
E. L. Hallin et al. Phys. Rev. C **48** 1497 (1993)  
Circles: MAMI,  
V Olmos de Leon et al. Eur. Phys. J. A **10** 207 (2001)  
Dotted curves etc. different parts of calc.  
Solid curve with error band, final calc

# Existing data and model predictions



Circles: MAMI, V Olmos de Leon et al. Eur. Phys. J. A **10** 207 (2001)

Squares: SAL, E. L. Hallin et al. Phys. Rev. C **48** 1497 (1993)

The curves are: Klein–Nishina (i.e, Compton scattering off a classical pointlike particle with the charge and mass of the proton) — dotted, Born graphs and Wess-Zumino-Witten (WZW)-anomaly — green dashed, adding the  $p_3 \pi N$  loop contributions of BPT— blue dash-dotted. The result of adding the contributions, i.e., the complete NNLO result, is shown by the red solid line with band

# Measurement of $\alpha$ and $\beta$

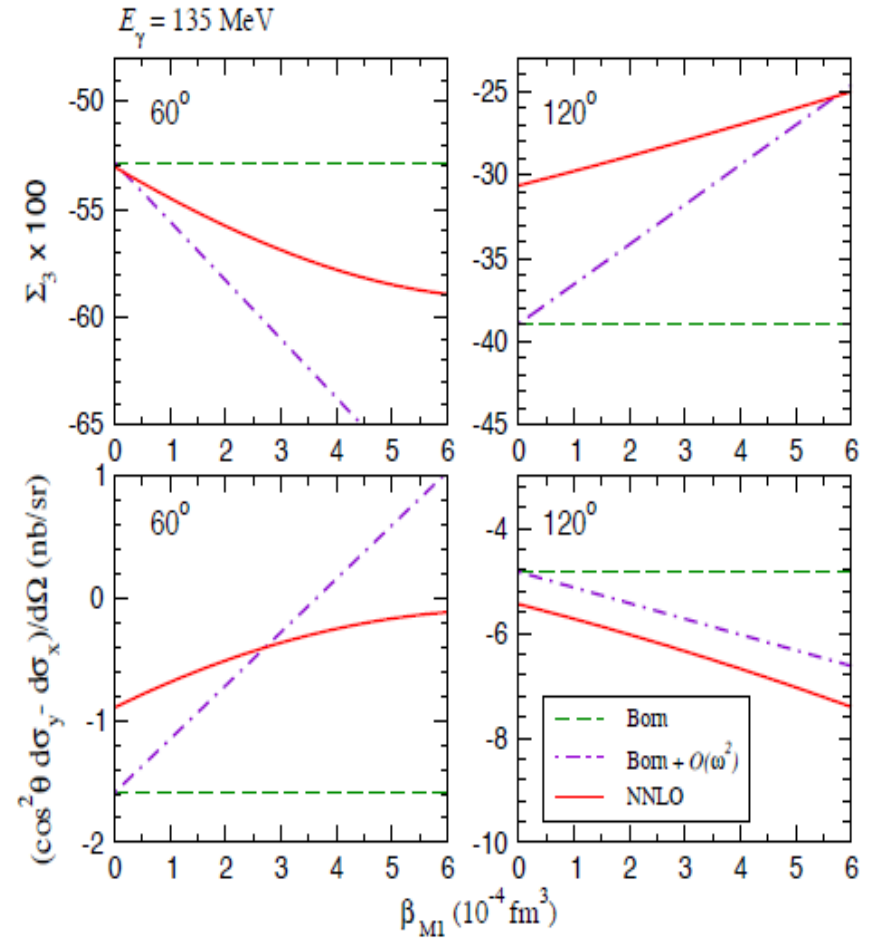
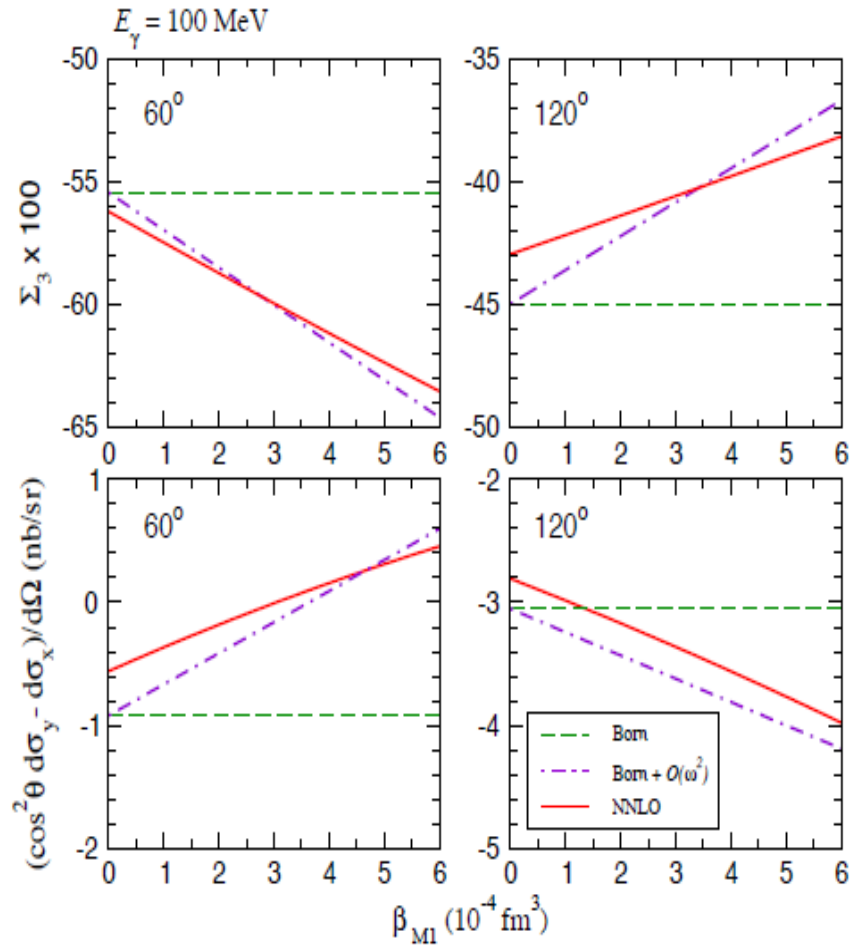
$$\Sigma_3 = \Sigma_3^{(B)} - \frac{4M\omega^2 \cos \theta \sin^2 \theta}{\alpha_{em}(1 + \cos^2 \theta)^2} \beta_{M1} + O(\omega^4), \quad (6)$$

where  $\Sigma_3^{(B)}$  is the pure Born contribution, while

$$\omega = \frac{s - M^2 + \frac{1}{2}t}{\sqrt{4M^2 - t}}, \quad \theta = \arccos \left( 1 + \frac{t}{2\omega^2} \right) \quad (7)$$

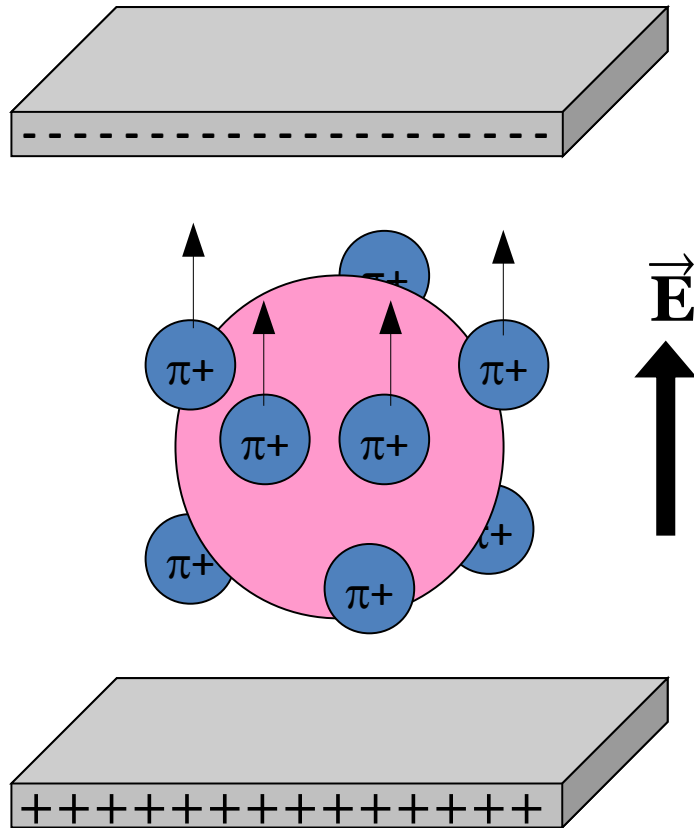
are the photon energy and scattering angle in the Breit (brick-wall) reference frame. In fact, to this order in the LEX the formula is valid for  $\omega$  and  $\theta$  being the energy and angle in the lab or center-of-mass frame.

# Measurement of $\alpha$ and $\beta$

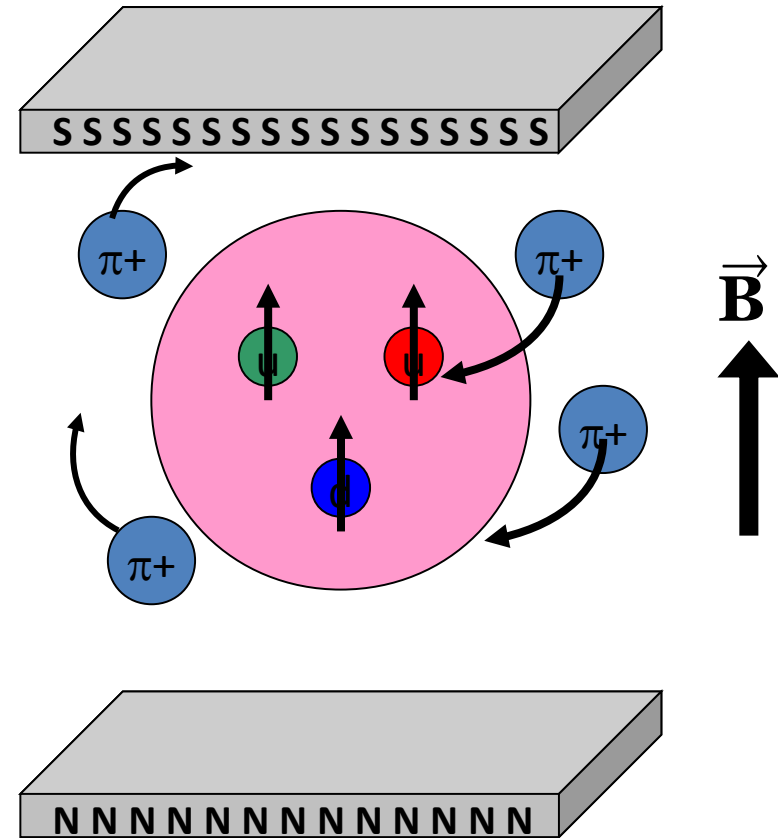


# Scalar polarizabilities

## Proton Electric Polarizability



## Proton Magnetic Polarizability

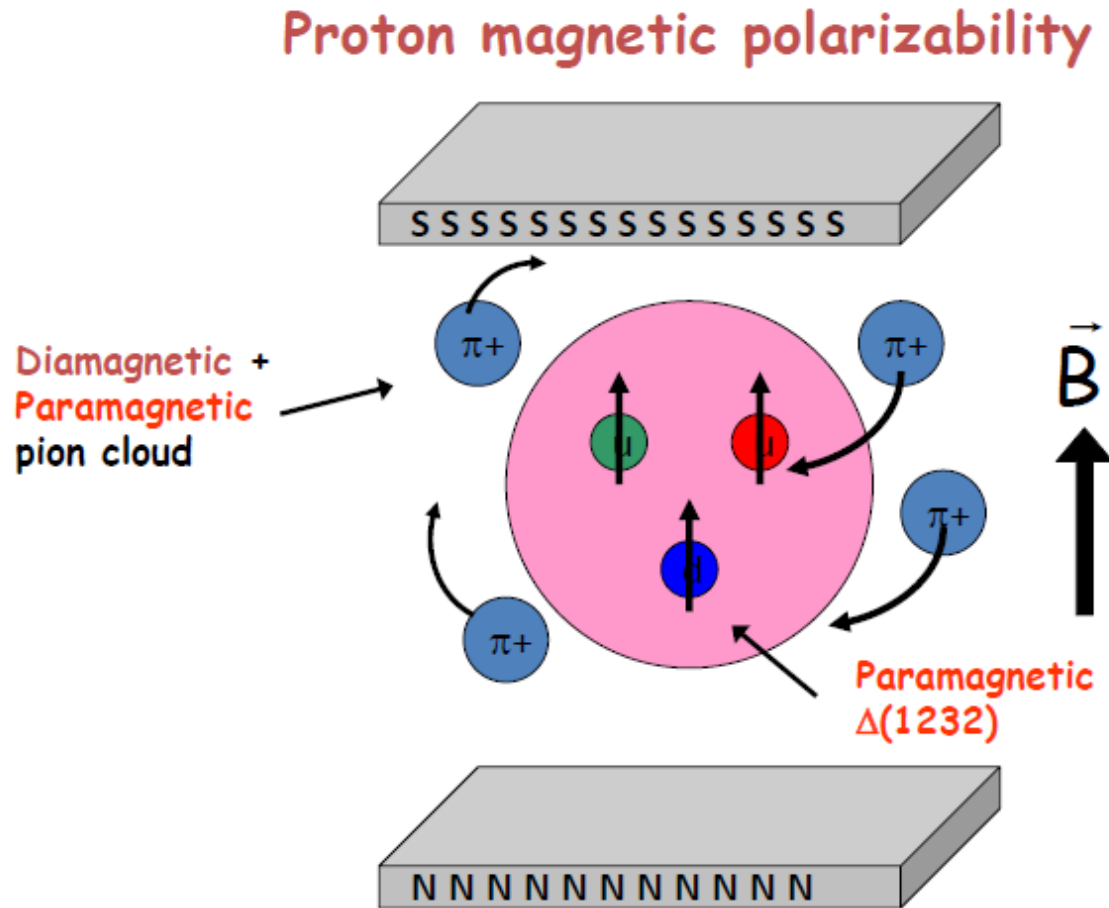


- $\alpha$ : electric polarizability
- Proton between charged parallel plates: “stretchability”

- $\beta$ : magnetic polarizability
- Proton between poles of a magnet: “alignability”



# First look in December 2012 data

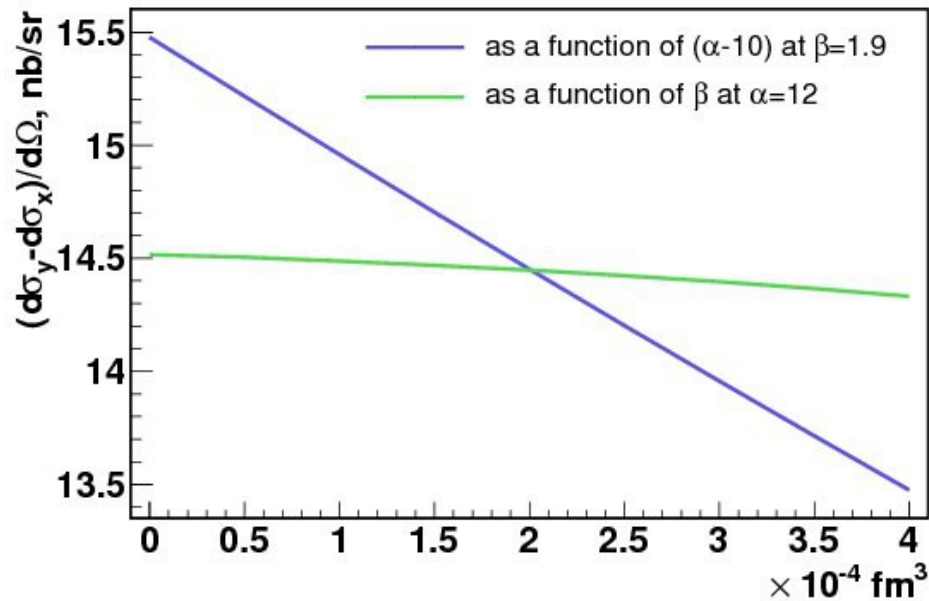


Magnetic polarizability: proton between poles of a magnetic

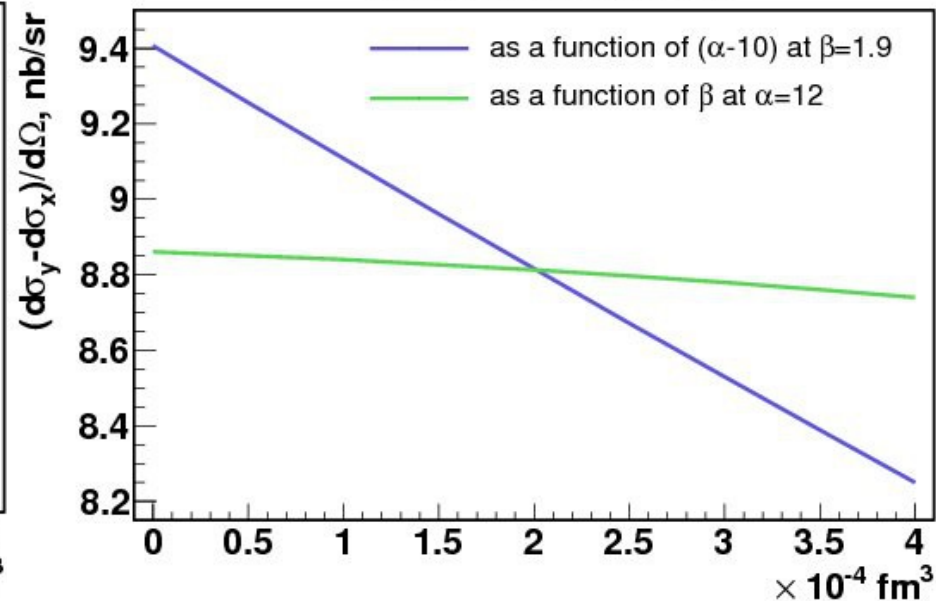
# Rory Miskimen (Bosen 2009)

# Sensitivity to $\alpha$

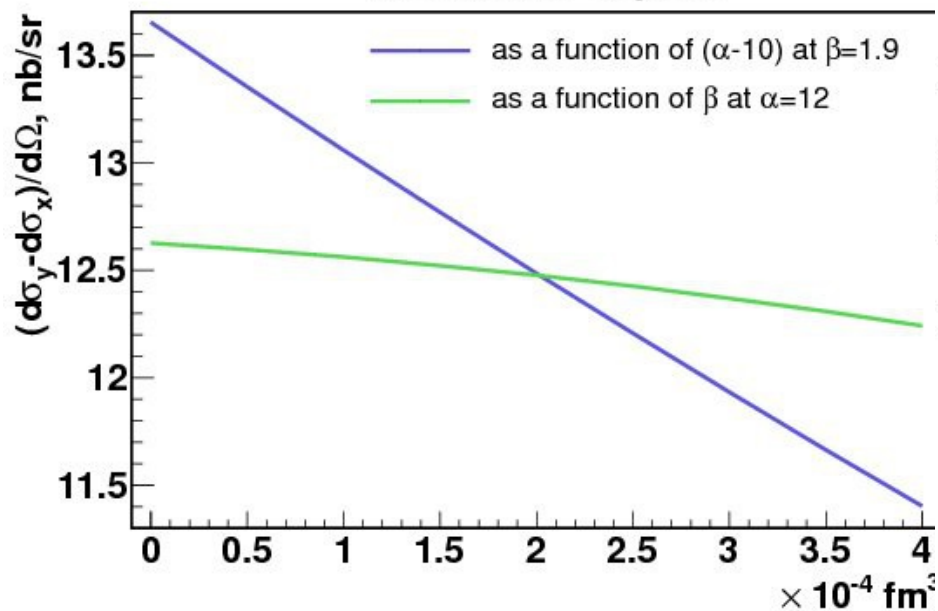
110 MeV, 90 degrees



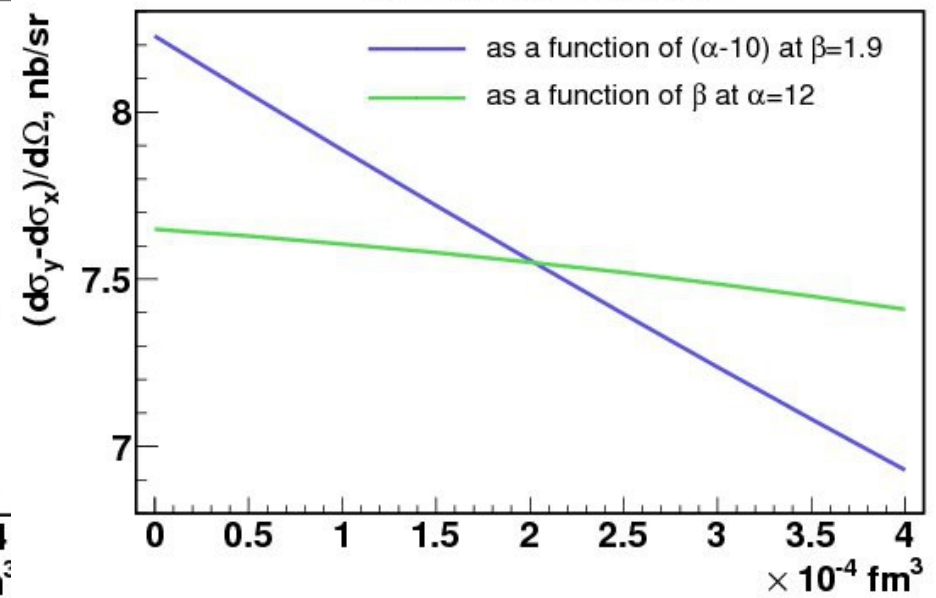
110 MeV, 125 degrees



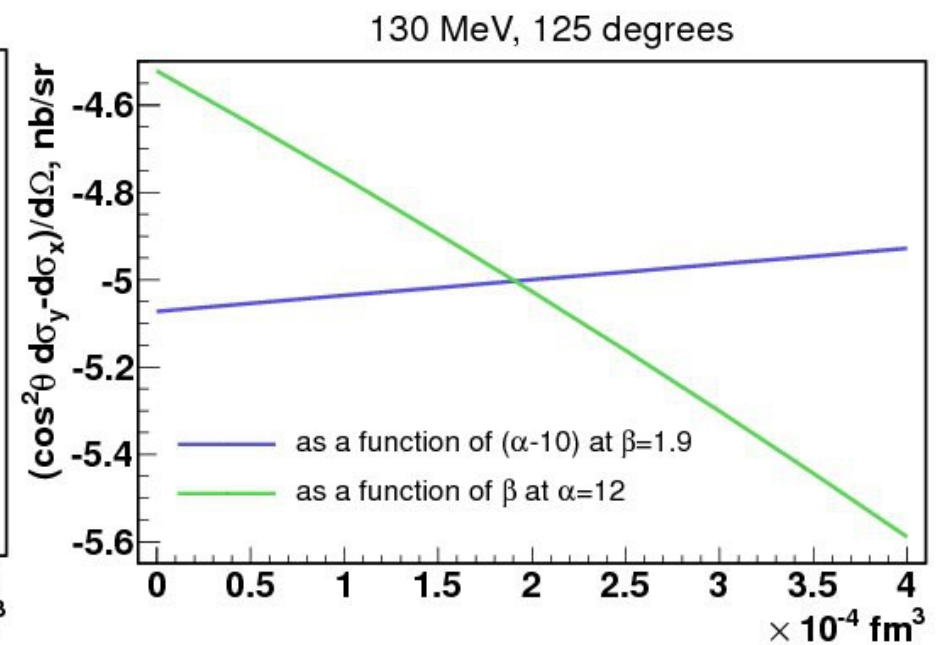
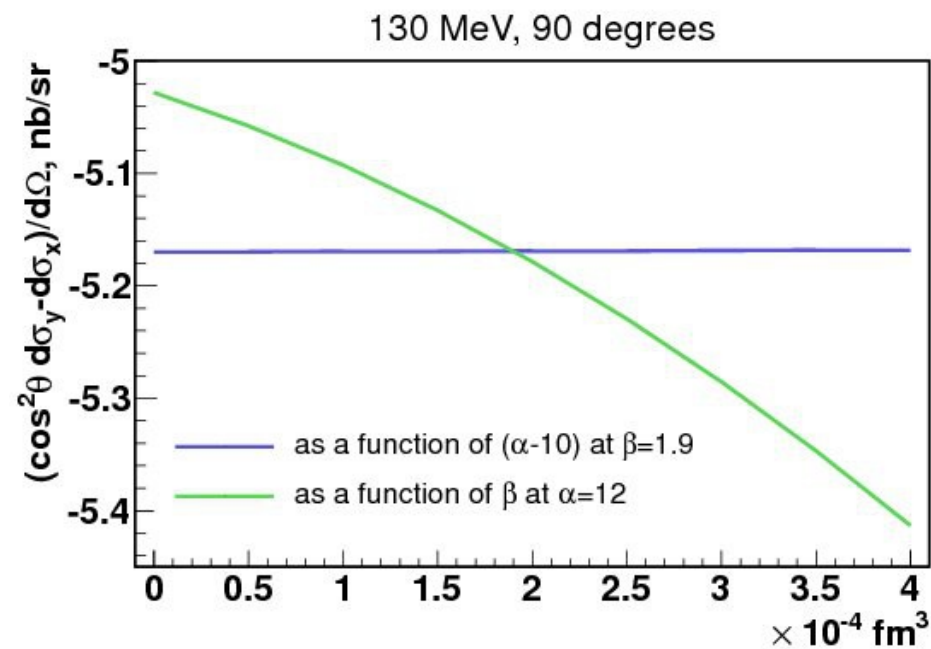
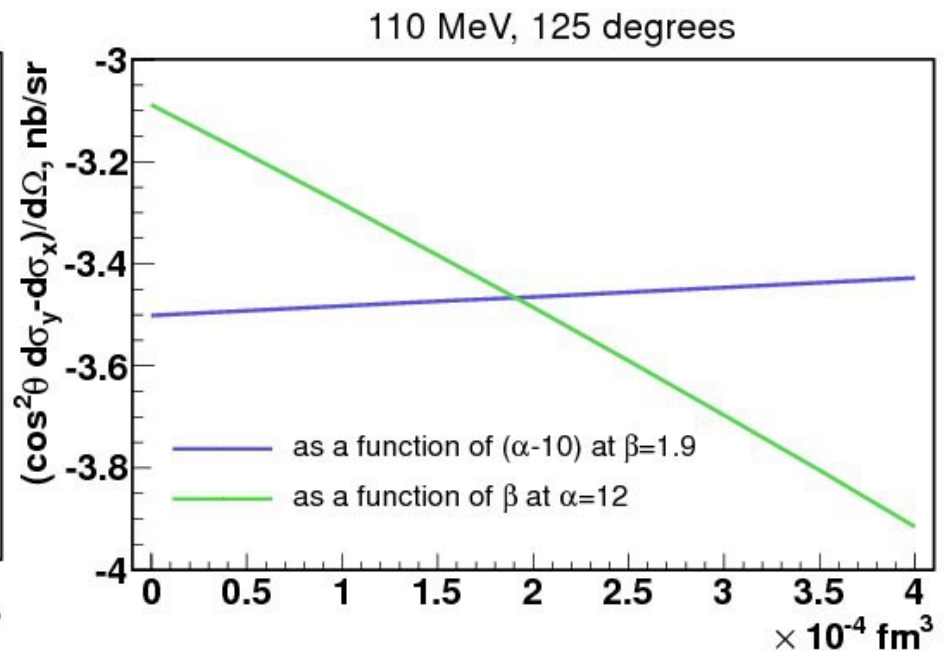
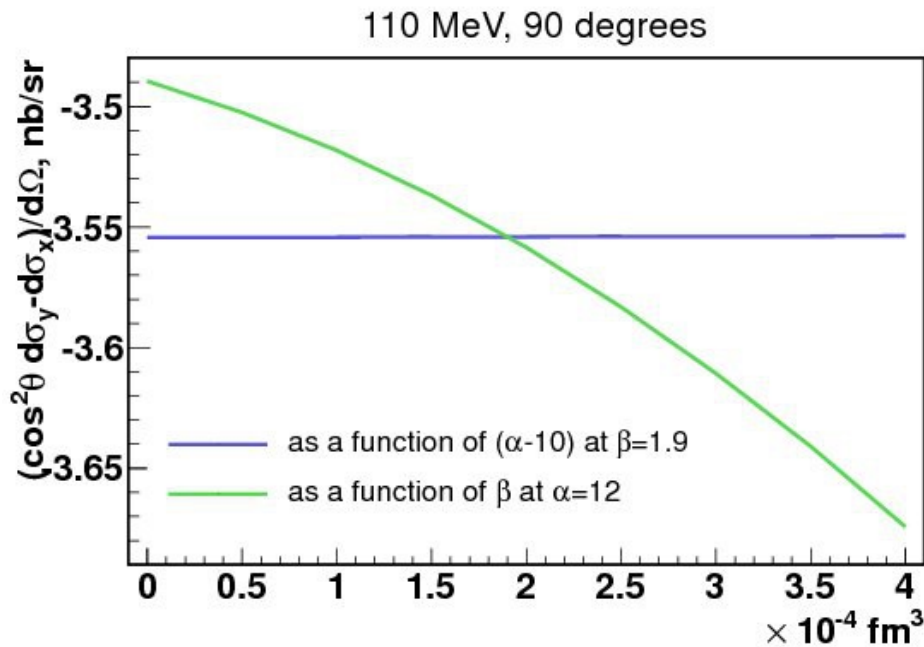
130 MeV, 90 degrees



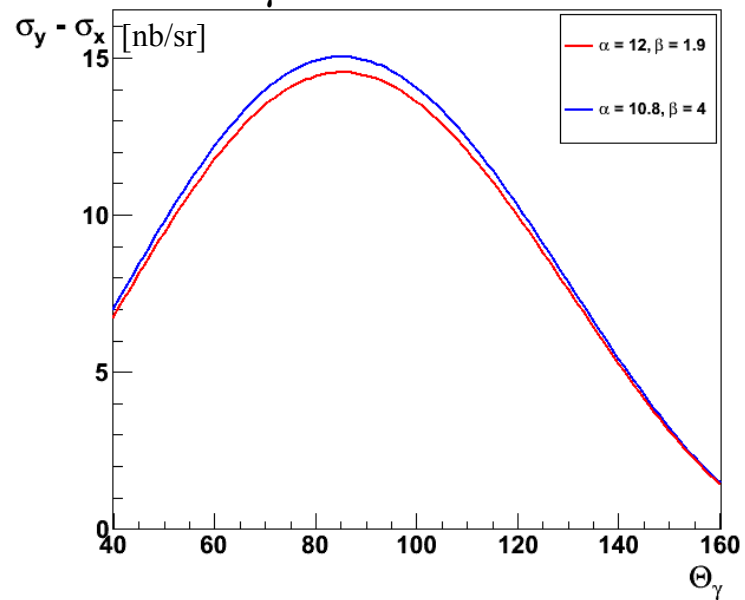
130 MeV, 125 degrees



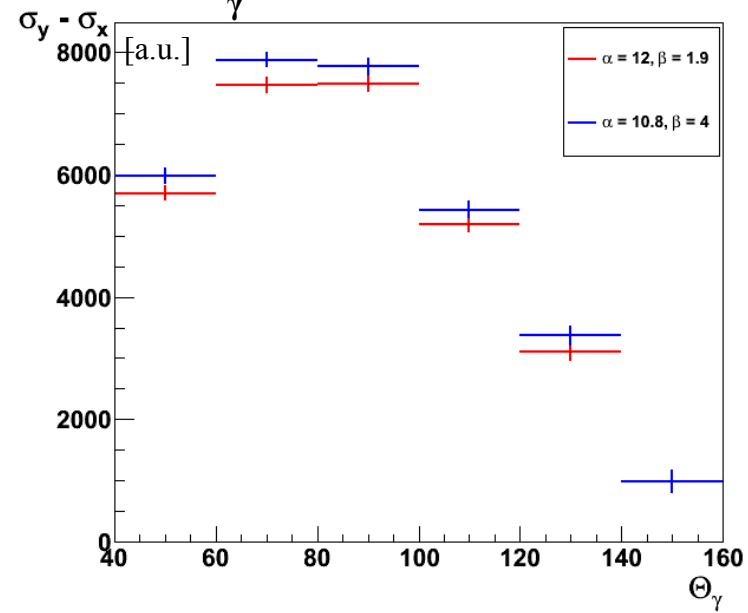
# Sensitivity to $\beta$



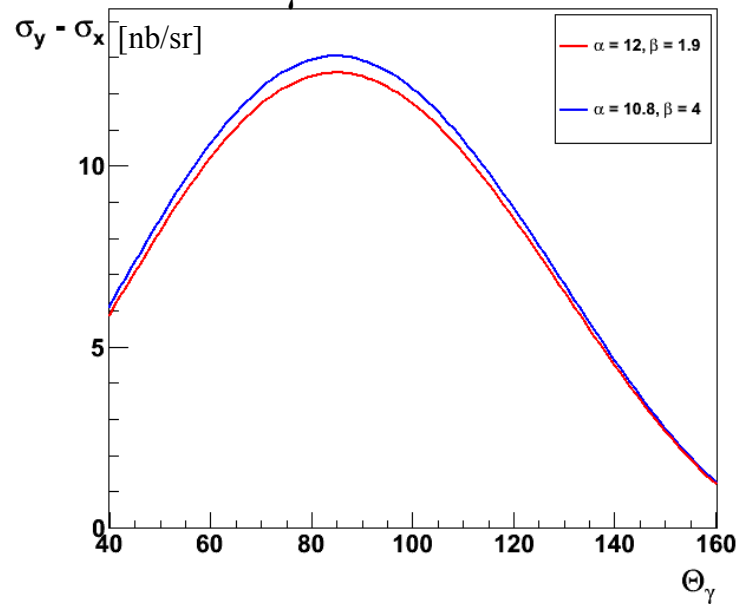
**$E_\gamma = 110 \text{ MeV}$**



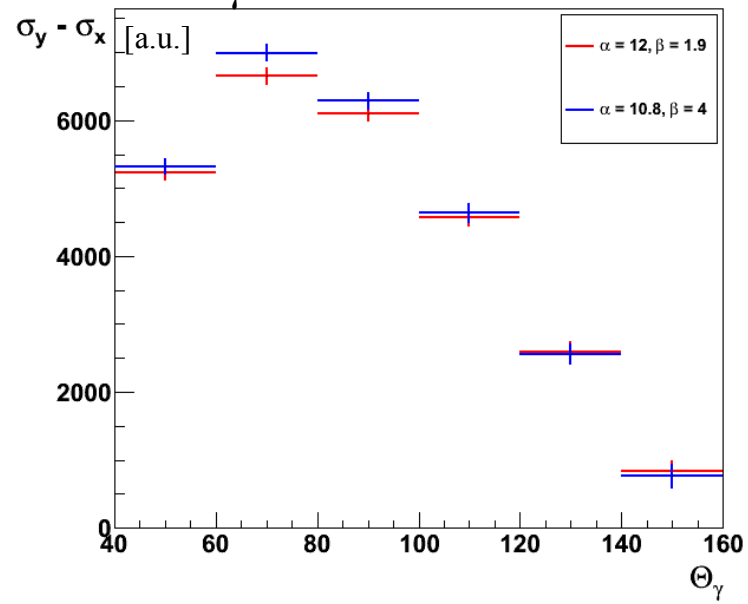
**$E_\gamma = 105 - 115 \text{ MeV}$**



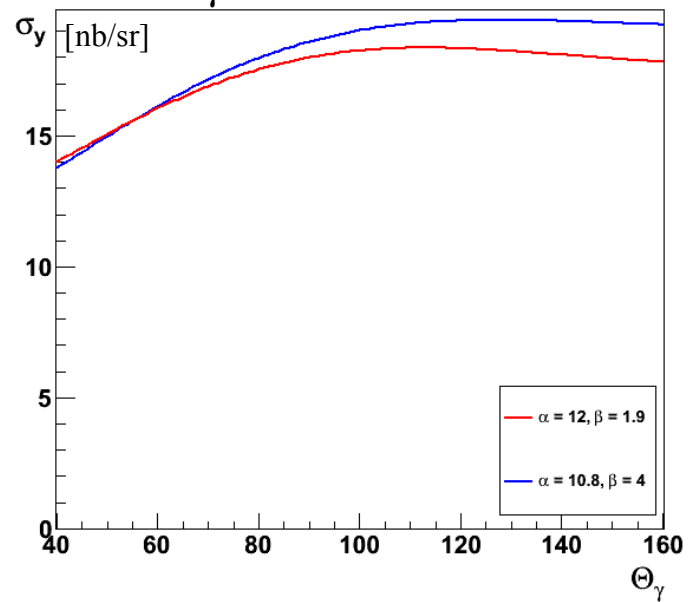
**$E_\gamma = 130 \text{ MeV}$**



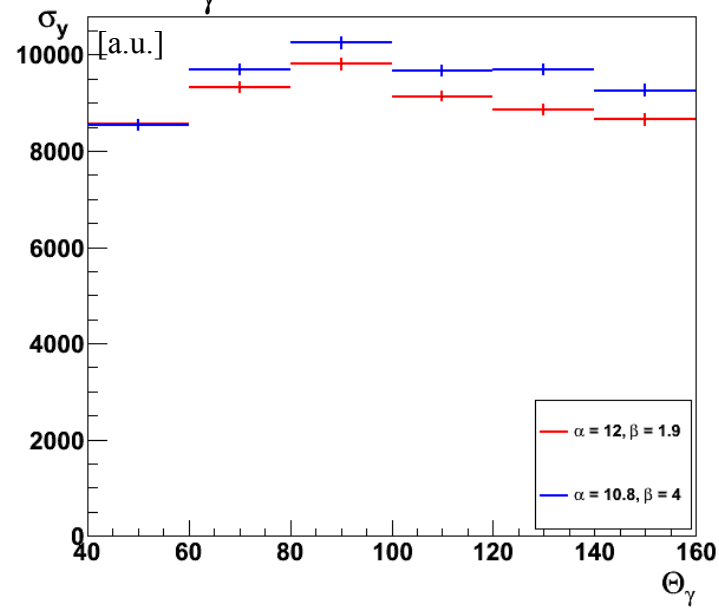
**$E_\gamma = 125 - 135 \text{ MeV}$**



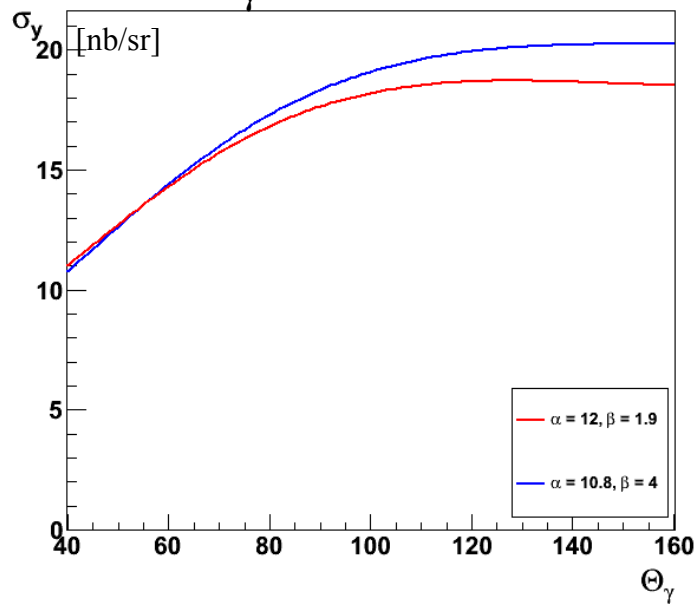
**$E_\gamma = 110 \text{ MeV}$**



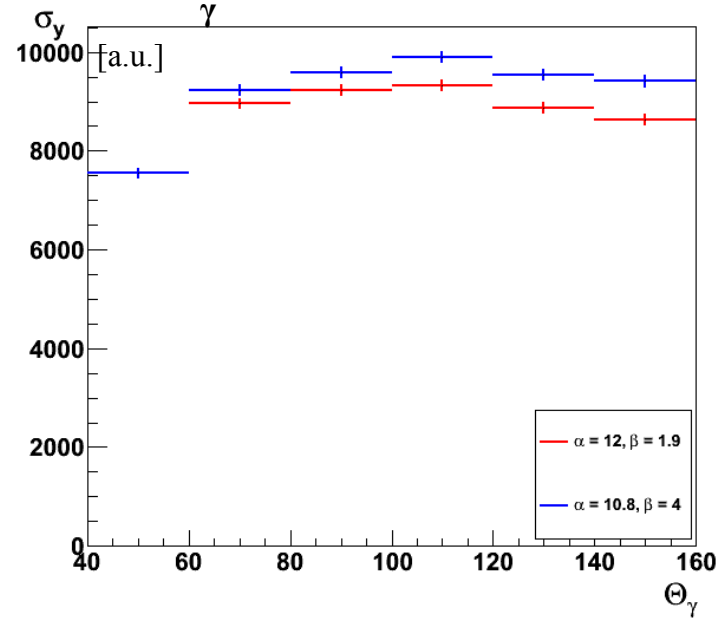
**$E_\gamma = 105 - 115 \text{ MeV}$**



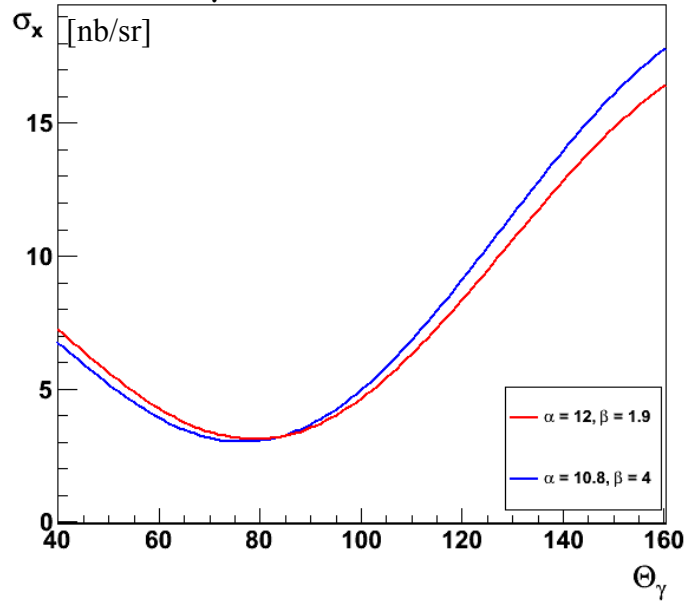
**$E_\gamma = 130 \text{ MeV}$**



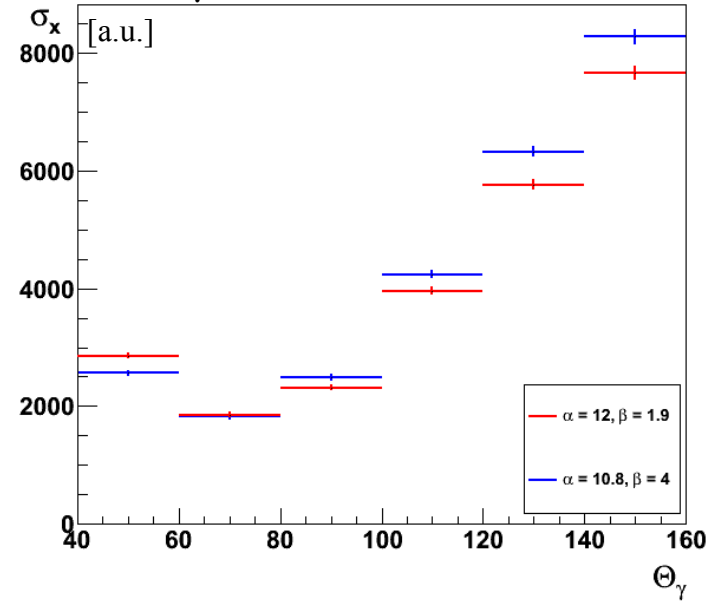
**$E_\gamma = 125 - 135 \text{ MeV}$**



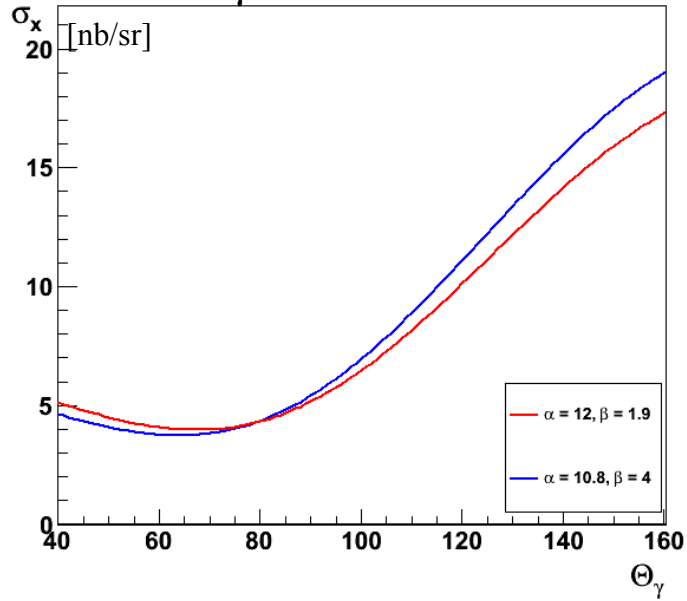
**$E_\gamma = 110 \text{ MeV}$**



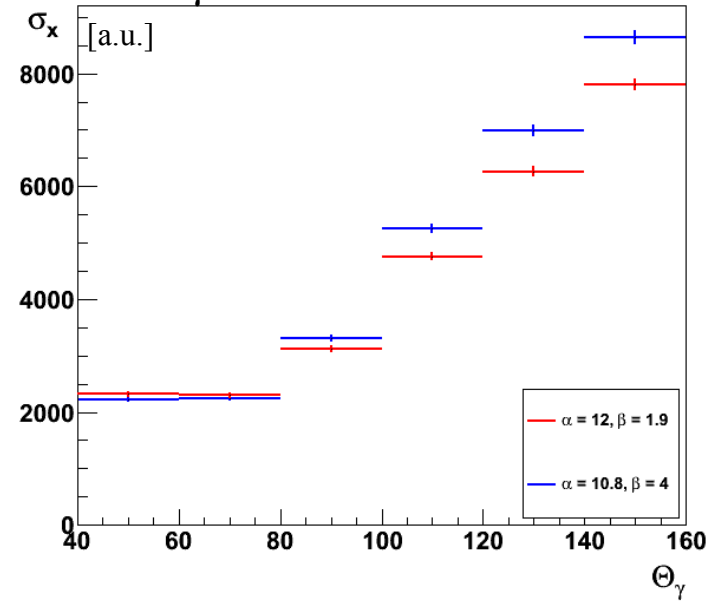
**$E_\gamma = 105 - 115 \text{ MeV}$**

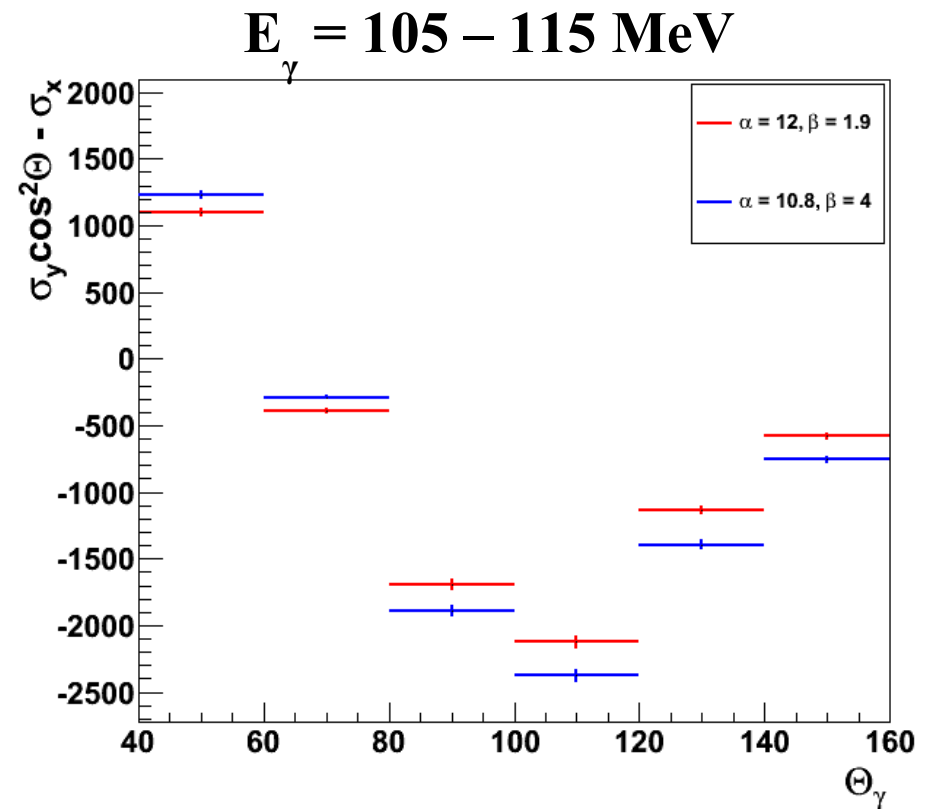
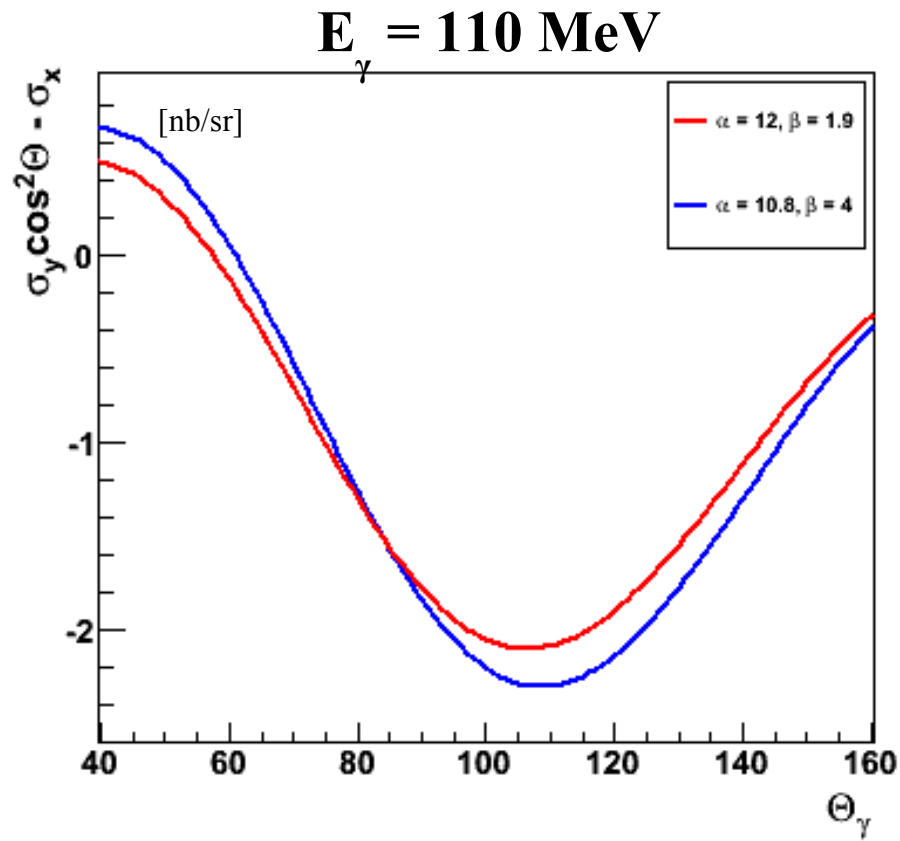


**$E_\gamma = 130 \text{ MeV}$**



**$E_\gamma = 125 - 135 \text{ MeV}$**

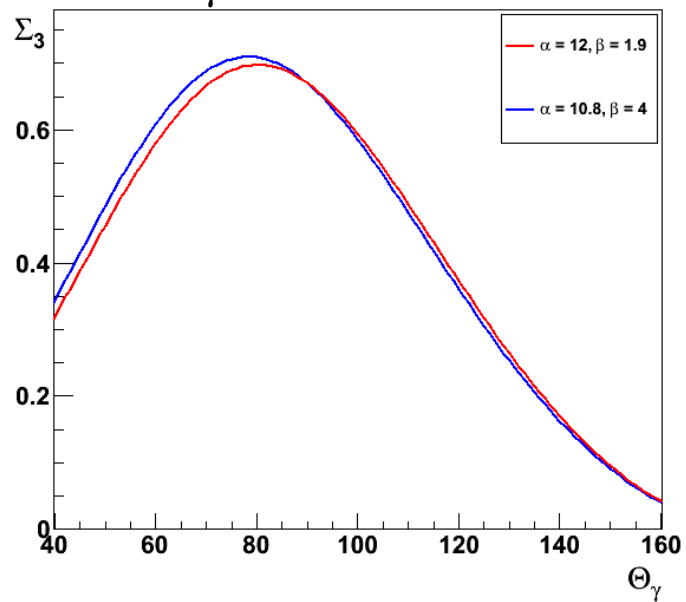




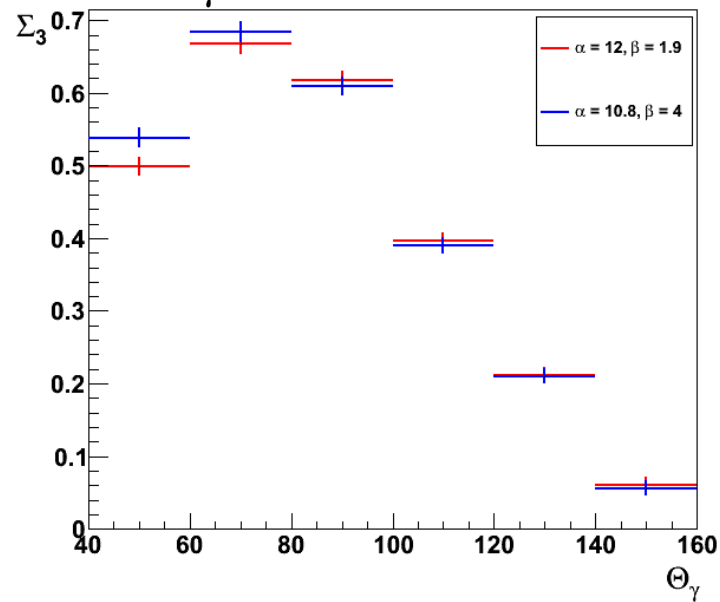
New data will allow to distinguish between different predictions!

- Independent measurement of  $\alpha$  and  $\beta$
- First measurement of  $\alpha$  and  $\beta$  using polarization observables

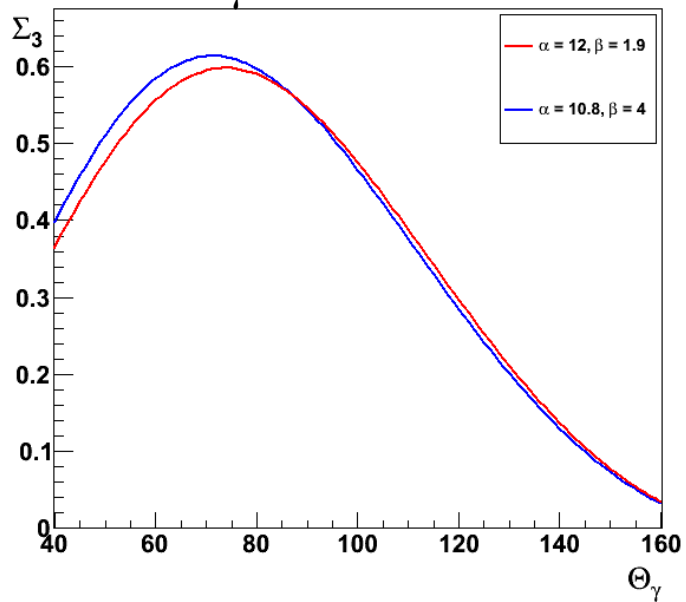
**$E_\gamma = 110 \text{ MeV}$**



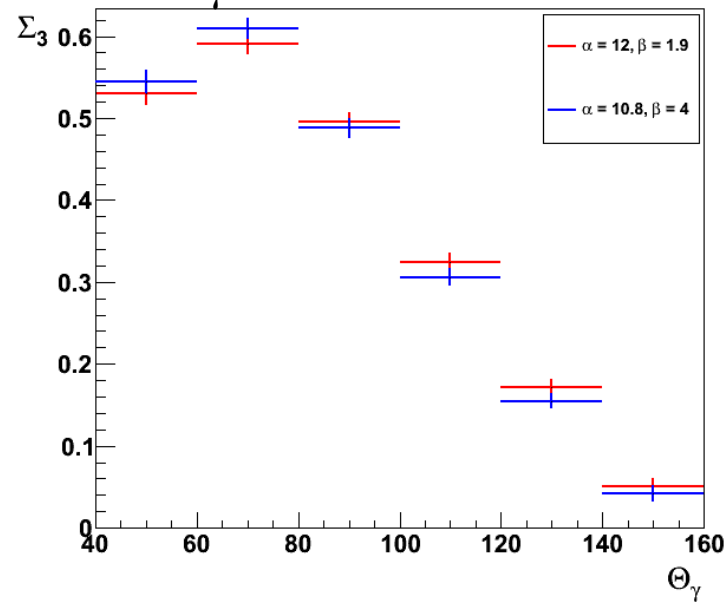
**$E_\gamma = 105 - 115 \text{ MeV}$**



**$E_\gamma = 130 \text{ MeV}$**



**$E_\gamma = 125 - 135 \text{ MeV}$**





# Kinematics

